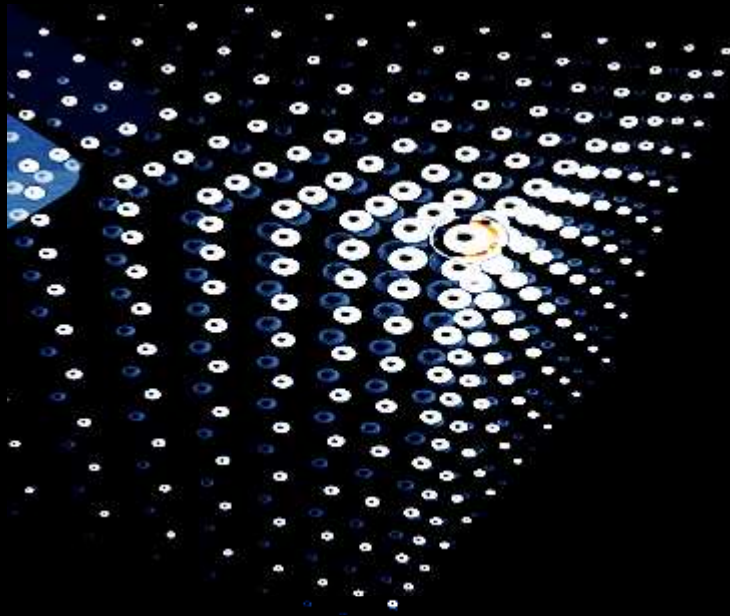




# **Transforming Metamaterials**

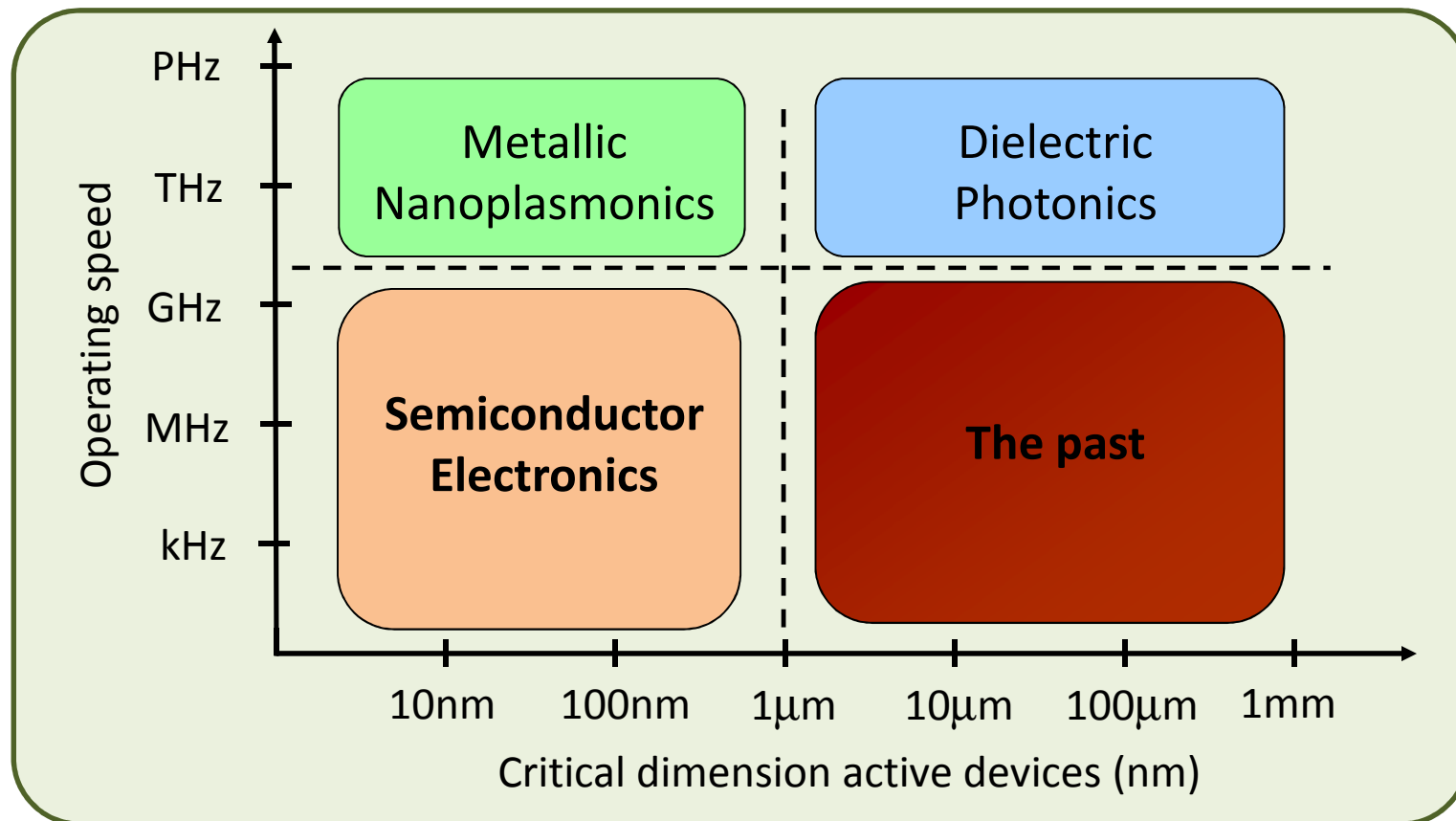
Vladimir M. Shalaev  
Purdue University

# Outline

- ❖ **Electrical Metamaterials (Plasmonics): A Route to Nanophotonics**
- ❖ **New Plasmonic Materials**
- ❖ **Negative-Index Metamaterials**
- ❖ **Chiral and Stereo- Metamaterials**
- ❖ **Active and Loss-Free Metamaterials**
- ❖ **Metamaterials for Sensing**
- ❖ **Tunable, Ultrafast, and Nonlinear Metamaterials**
- ❖ **Quantum Optics with Metamaterials**
- ❖ **Transformation Optics: Cloaking, TO-SPP, Fish-Eye & Eaton Lenses**
- ❖ **Metamaterial “Multiverse”**

# **Electrical Metamaterials (Plasmonics): A Route to Nanophotonics**

# Why Plasmonics/Electric $\epsilon$ -MMs ?

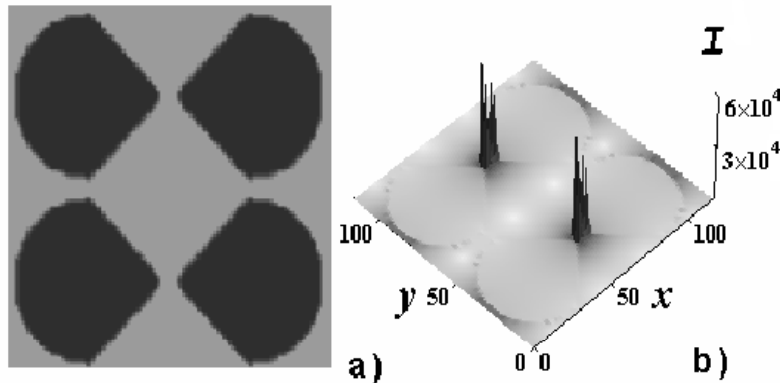


- Plasmonics will enable an improved synergy between electronic and photonic devices
  - Plasmonics naturally interfaces with similar size electronic components
  - Plasmonics naturally interfaces with similar operating speed photonic networks



# Optical Antennae: Focusing Light to Nanoscale

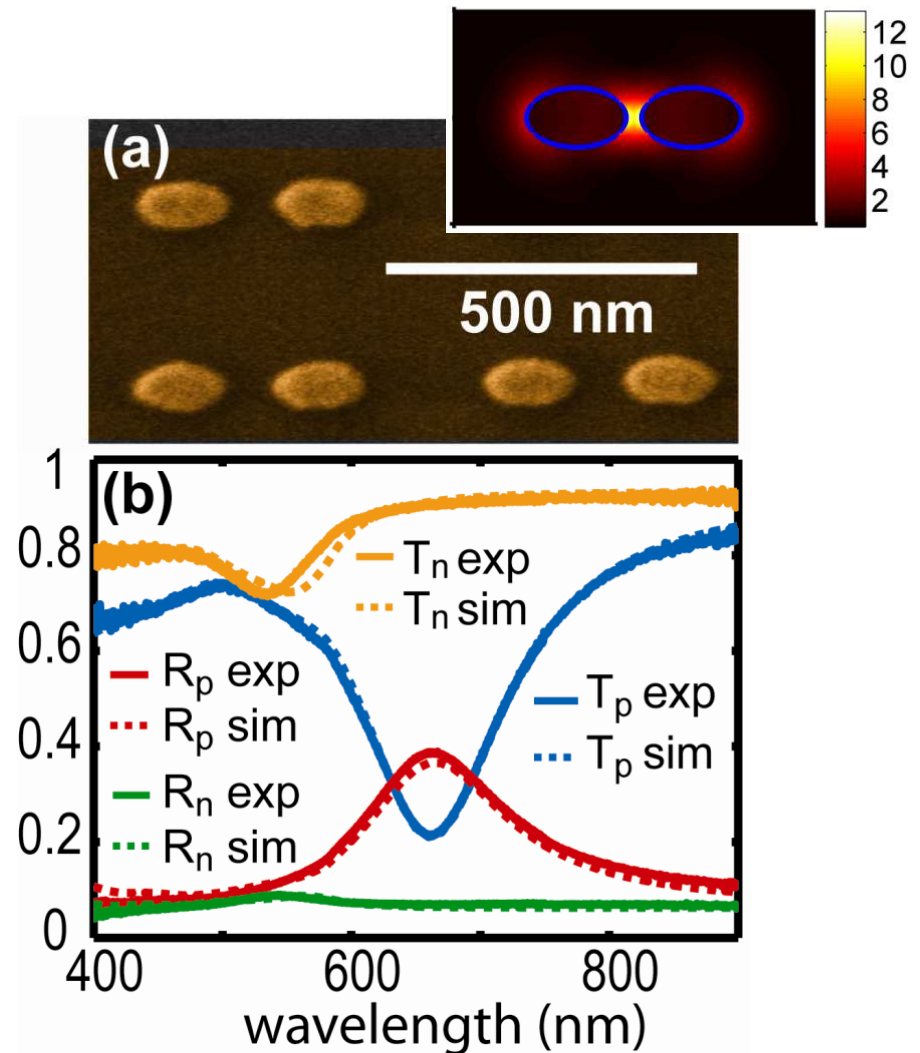
## [ Bow-tie antennas ]



from LC-contour to nanophotonic circuits  
(Engheta – ‘metatronics’)

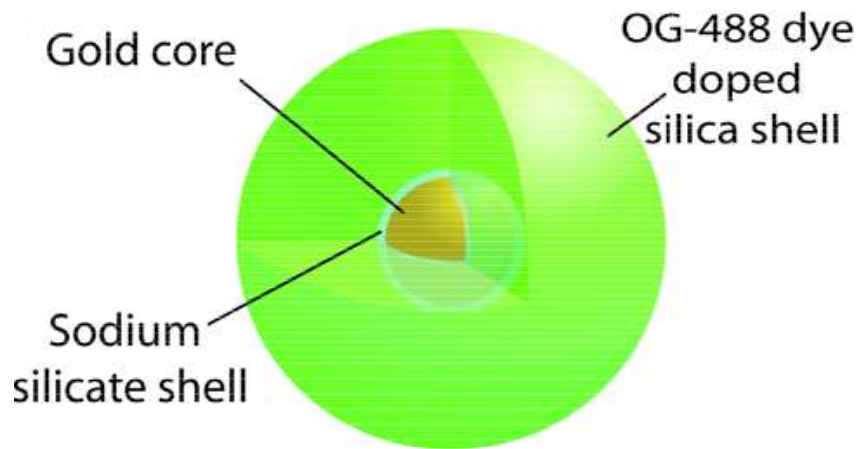
### Other Applications:

Sensors

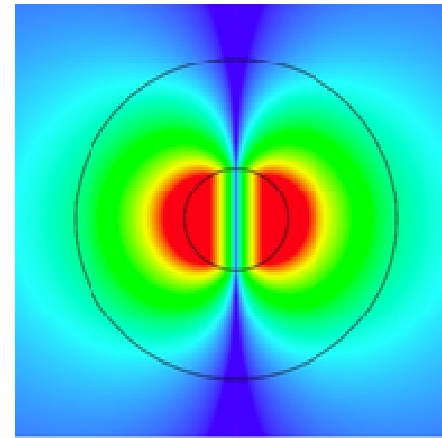


Other nanoantenna work: van Hulst, Polman, Brongersma, Capasso,...

# Optical Nanolaser Enabled by SPASER



Related prior theory:  
Stockman (spaser)

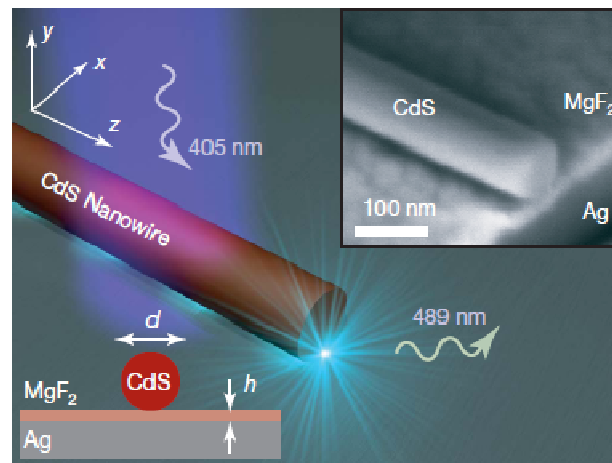


Noginov, Shalaev, Wiesner groups, *Nature* (2009)

NSU-Purdue-Cornell; *Nature* (2009)

Zhang's group: Plasmon laser  
(*Nature*, 2009)

Room-T Plasmon Laser  
(*Nature Materials*, 2010)



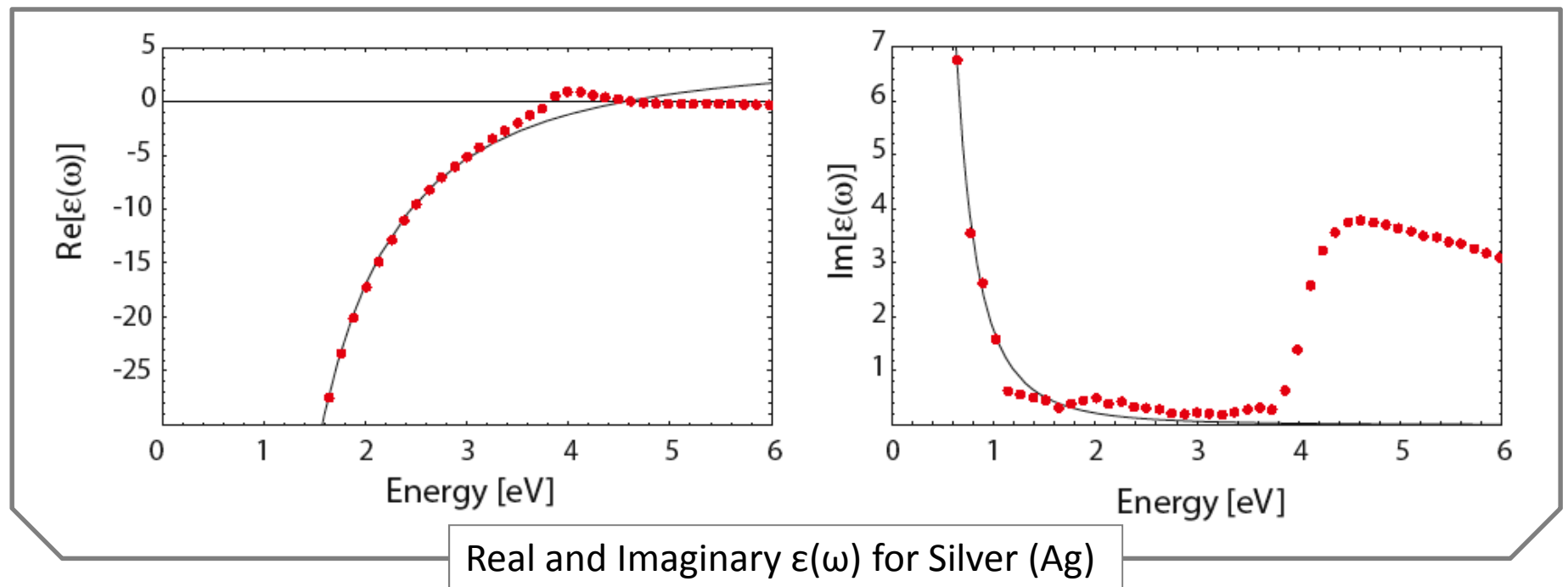
Optical MOSFET  
(Stockman)

# **Toward Better Materials & Fabrication**

# Challenges

## Conventional plasmonics: *Gold and Silver*

- Large losses in near-IR and visible ranges
- Interband transitions
- Surface roughness, grain boundaries, etc...

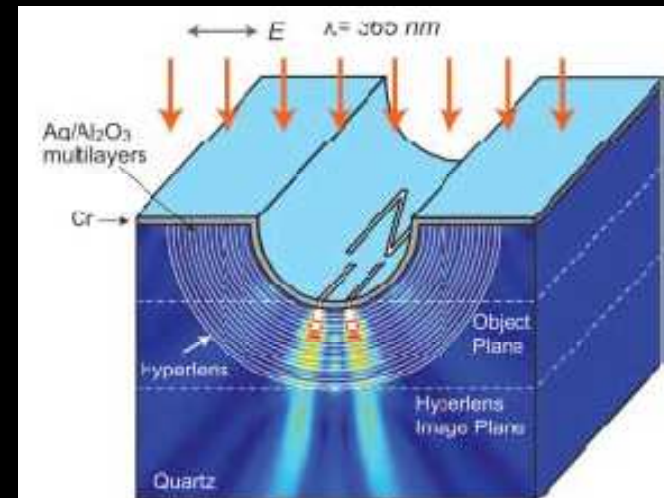


Johnson and Christy (dots) (1972)  
Stefan Maier, Plasmonic Fundamentals and Applications p. 17 (Drude model fit) (2007)

# Challenges

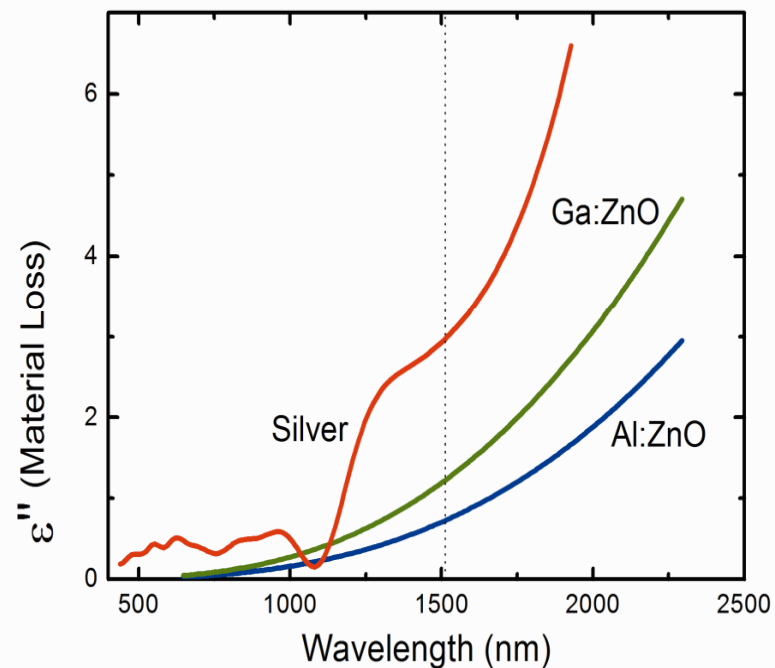
## Conventional plasmonics: *Gold and Silver*

- Large losses in near-IR and visible ranges
- Emerging new fields such as Transformational Optics have different requirements
- Effective permittivity nearly zero: e.g. optical cloaks, hyperlens etc.
- Real permittivity of metals must be comparable to that of dielectrics

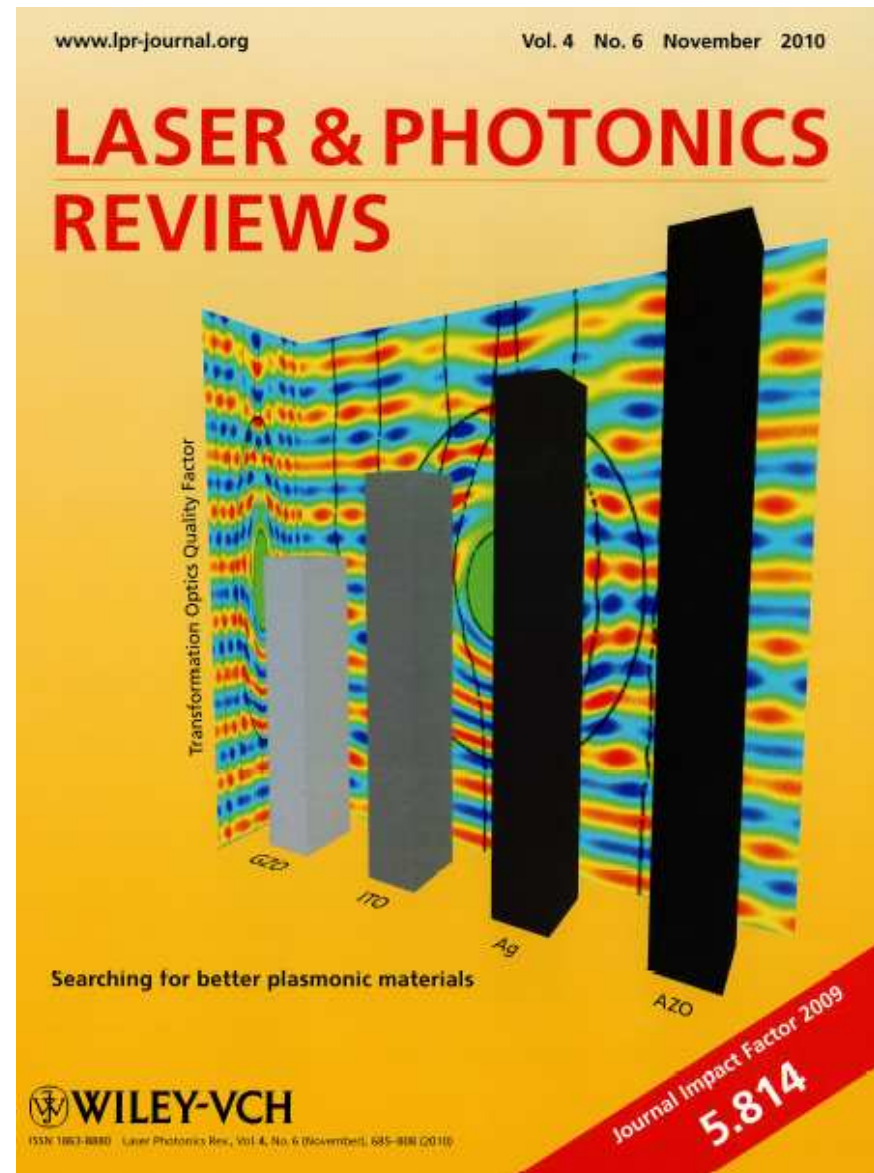


# Alternative Plasmonic Materials

## Transparent Conductive Oxides



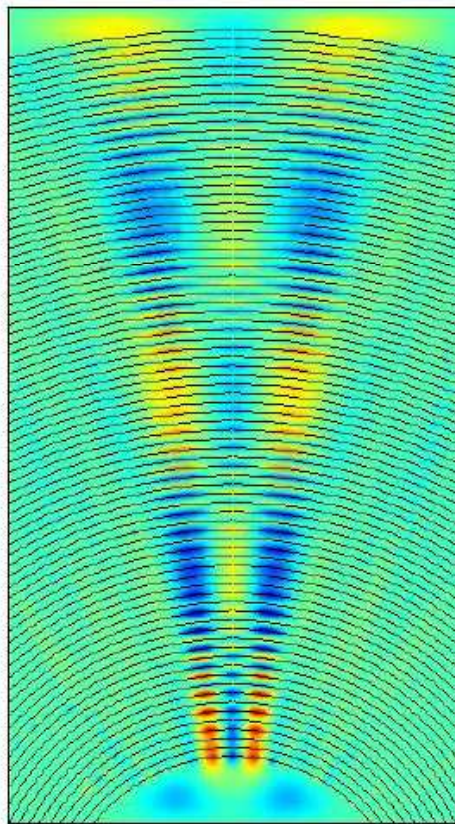
P. R. West et. al, Lasers & Photon. Rev 4, 795 (2010)  
(Boltasseva group)





# There are Other Materials!

## Figure of Merit of Hyperlens @ 1.55 $\mu\text{m}$



Performance of  
HMM devices:  
(A. Hoffman, Nature  
Materials 6(2007) 946–950)

$$\text{FOM} = \text{Re}\{k_{\perp}\} / \text{Im}\{k_{\perp}\}$$

## HMM Performance: Figure of merit for TiN

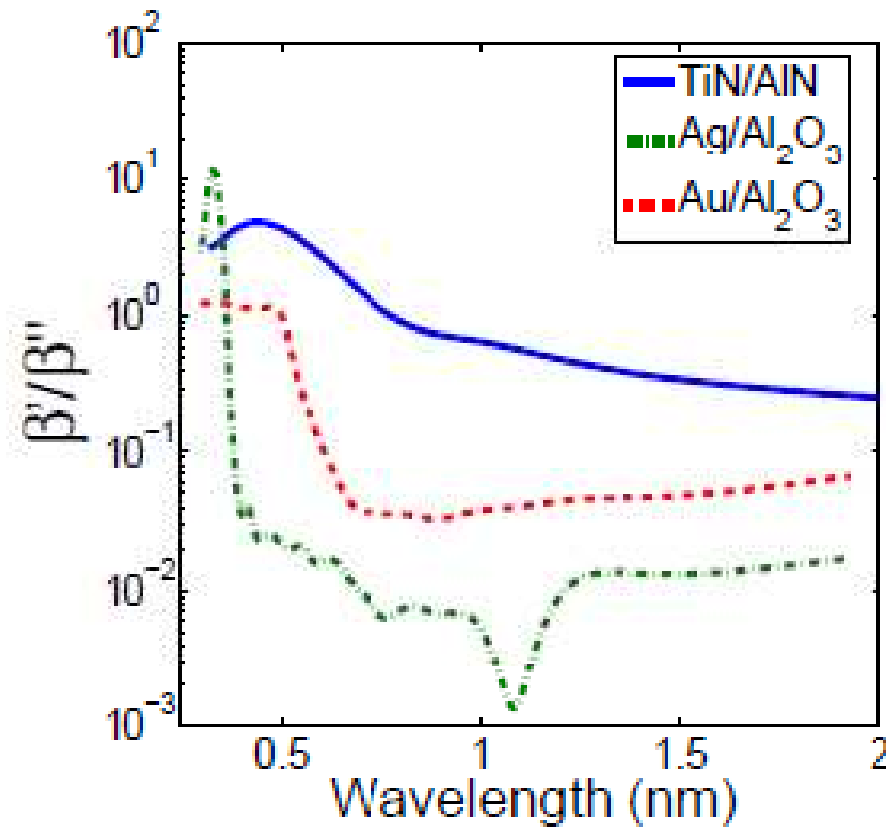
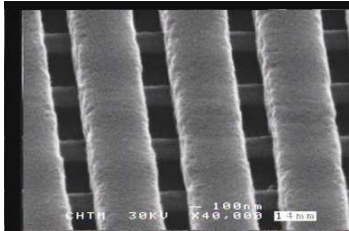


Figure-of-merit of HMMs formed by alternating, sub-wavelength layers of TiN/AlN, Ag/alumina and Au/alumina

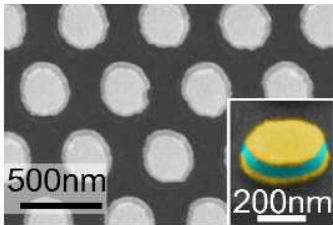


# Progress in Large-Scale & 3D Fabrication

## [Interference Lithography]

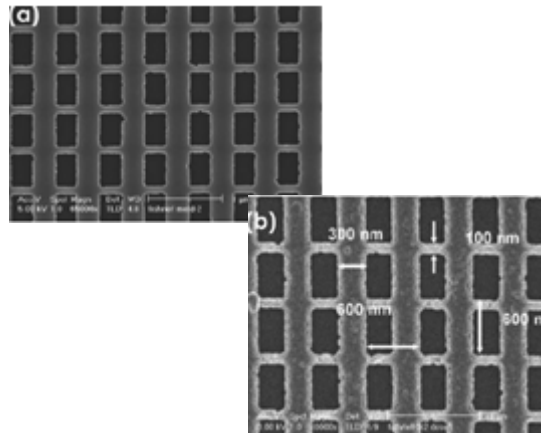


Z. Ku & SRJ Brueck, Opt. Exp. **15**, 4515 (2007)



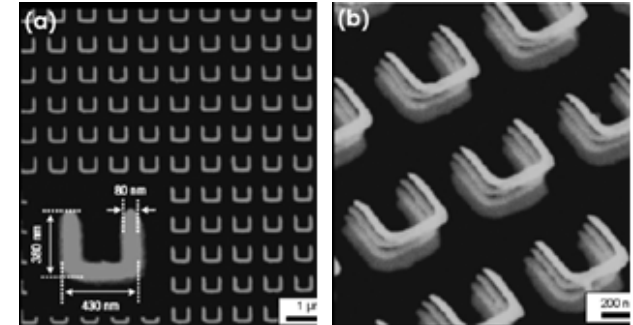
Nils Feth et. al, Opt. Exp. **15**, 501 (2007) (Wegener group)

## [Nanoimprint Lithography]



W. Wu et. al, Appl. Phys. A **87**, 143 (2007)

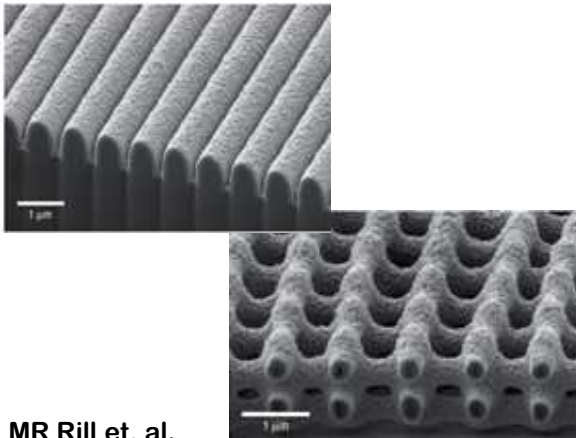
## [Building layer-by-layer]



Na Liu et. al, Nat. Mater. **7**, 31 (2007)  
(Giessen group)

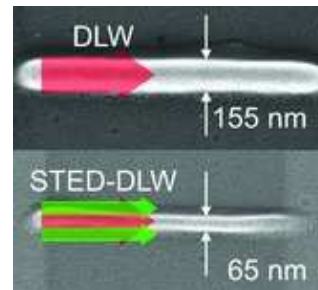
**3D**

## [Direct Laser Writing]



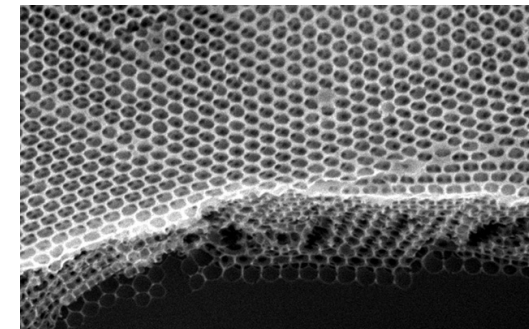
MR Rill et. al,  
Nat. Mater. **5**, 743 (2008) (Wegener group)

## [STED-Direct Laser Writing]



J. Fischer et. al, Adv. Mater. **22**, 3578 (2010)  
(Wegener group)

## [Self-assembly]

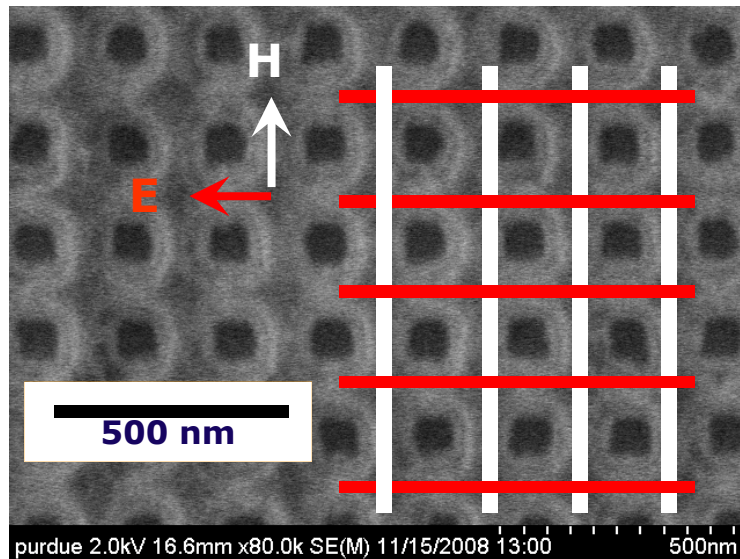


JF Galisteo et. al, J. Opt. A **7**, 244 (2005)

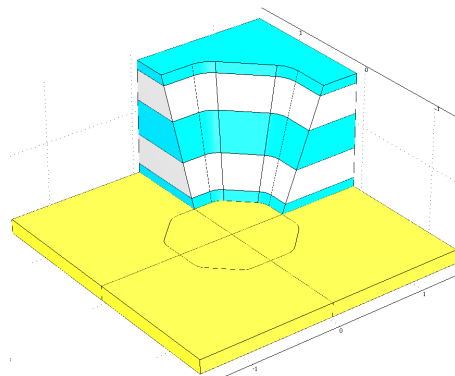
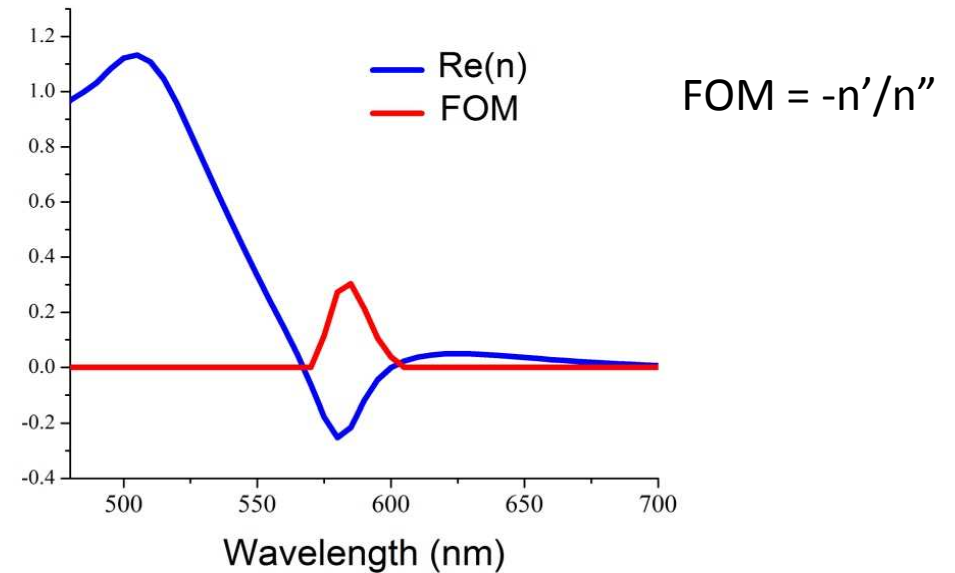
# **Optical Negative-Index Metamaterials**

# Negative Index for Yellow Light

Periodicity, E: 220 nm; H: 220 nm



$n' = -0.25$ , FOM = 0.3, at 580 nm



**Stacking:**

8 nm of  $\text{Al}_2\text{O}_3$   
43 nm of Ag  
45 nm of  $\text{Al}_2\text{O}_3$   
43 nm of Ag  
8 nm of  $\text{Al}_2\text{O}_3$

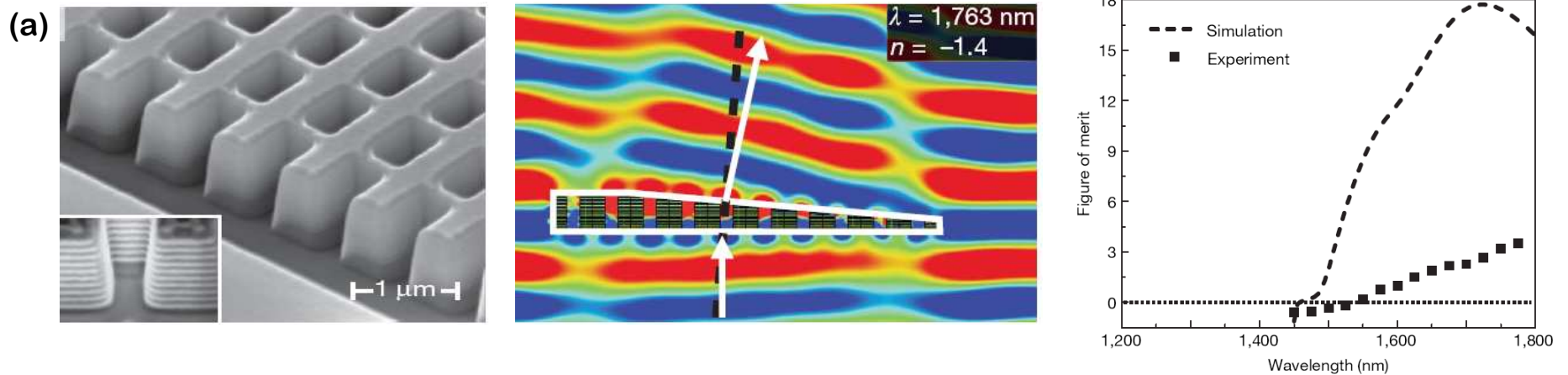
# Negative Refractive Index in Optics

| <i>Year and Research group</i> | <i>1st time posted and publication</i>                              | <i>Refractive index, <math>n'</math></i> | <i>Wavelength, <math>\lambda</math></i> | <i>Figure of Merit <math>F= n' /n''</math></i> | <i>Structure used</i>         |
|--------------------------------|---------------------------------------------------------------------|------------------------------------------|-----------------------------------------|------------------------------------------------|-------------------------------|
| <b>2005</b>                    |                                                                     |                                          |                                         |                                                |                               |
| <b>Purdue</b>                  | April 13 (2005)<br>arXiv:physics/0504091<br>Opt. Lett. (2005)       | −0.3                                     | 1.5 $\mu\text{m}$                       | 0.1                                            | Paired nanorods               |
| <b>UNM &amp; Columbia</b>      | April 28 (2005)<br>arXiv:physics/0504208<br>Phys. Rev. Lett. (2005) | −2                                       | 2.0 $\mu\text{m}$                       | 0.5                                            | Nano-fishnet with round voids |
| <b>2006</b>                    |                                                                     |                                          |                                         |                                                |                               |
| <b>UNM &amp; Columbia</b>      | J. of OSA B (2006)                                                  | −4                                       | 1.8 $\mu\text{m}$                       | 2.0                                            | Nano-fishnet with round voids |
| <b>Karlsruhe &amp; ISU</b>     | OL. (2006)                                                          | −1                                       | 1.4 $\mu\text{m}$                       | 3.0                                            | Nano-fishnet                  |
| <b>Karlsruhe &amp; ISU</b>     | OL (2006)                                                           | −0.6                                     | 780 nm                                  | 0.5                                            | Nano-fishnet                  |
| <b>Purdue</b>                  | MRS Bulletin (2008)                                                 | −0.8<br>−0.6                             | 725nm<br>710nm                          | 1.1<br>0.6                                     | Nano-fishnet                  |
| <b>Purdue</b>                  | OL (2009)                                                           | −0.25                                    | 580nm                                   | 0.3                                            | Nano-fishnet                  |

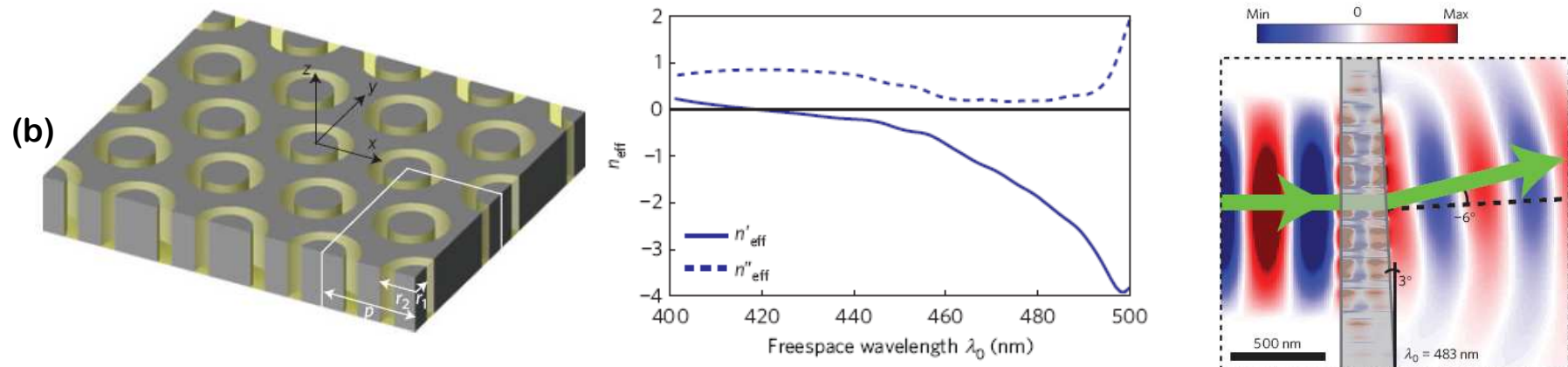
CalTech (Atwater): negative refraction in the visible for MIM waveguide SPPs (2007)

# Negative-Index Metamaterials (NIMs)

- Three-dimensional optical metamaterial with a negative refractive index



- A single-layer wide-angle negative-index metamaterial at visible frequencies



(a) Zhang group, Nature. 455, 376 (2008)

(b) S. P. Burgos, et al, Nature materials. (2010) (Polman-Atwater groups)

# **Chiral and Stereo- Metamaterials**

# Chiral Metamaterials

- Coupling effect between E-field and M-field (Chirality parameter[κ])

$$\begin{pmatrix} D \\ B \end{pmatrix} = \begin{pmatrix} \epsilon_0 \epsilon & -\frac{i\kappa}{c} \\ \frac{i\kappa}{c} & \mu_0 \mu \end{pmatrix} \begin{pmatrix} E \\ H \end{pmatrix}$$

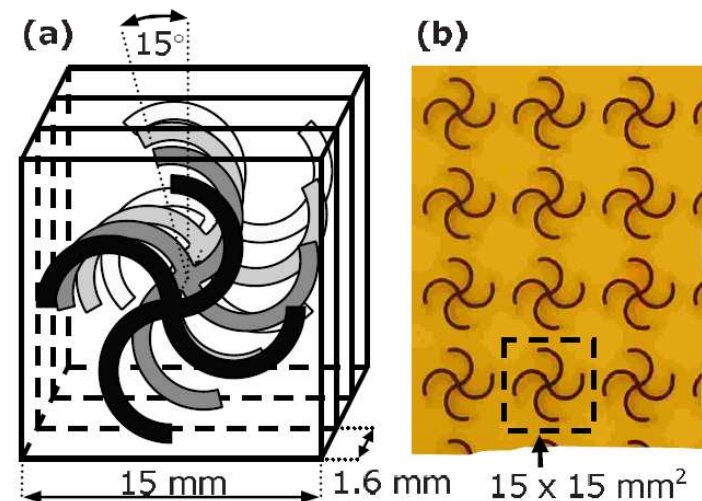
- Right circularly polarized (RCP) / Left circularly polarized (LCP)

$$\begin{aligned} k_{\pm} &= k_0(n \pm \kappa) \\ n_{\pm} &= n \pm \kappa \end{aligned}$$

## <Negative index refraction>

- without negative permittivity (ε)  
/negative permeability (μ)
- Chirality parameter (κ) >  $\sqrt{\epsilon\mu}$
- Refractive index for the LCP ⇒ negative

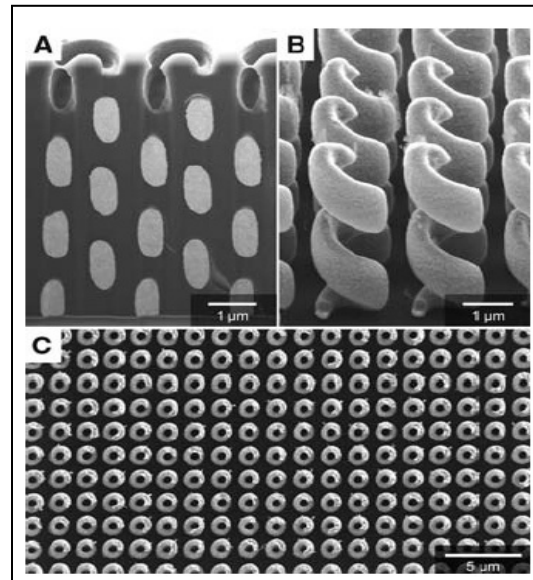
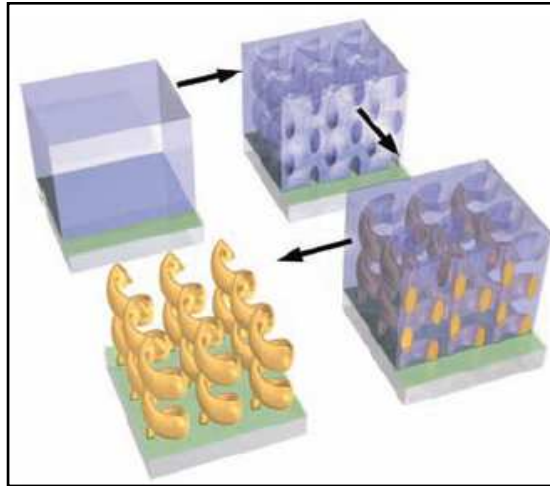
$$k_- < 0, \quad n_- < 0,$$





# 3-D Chiral Metamaterials

## [Fabrication process]

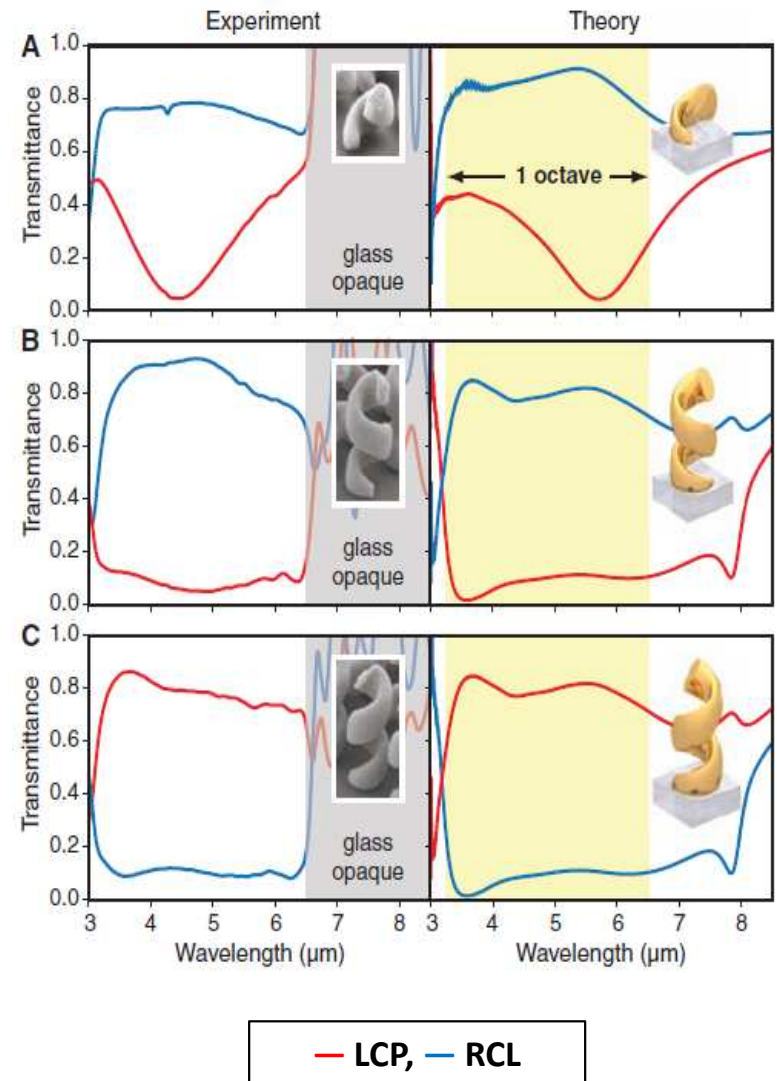


## [SEM images]

A Cross view

B Tilt angle view

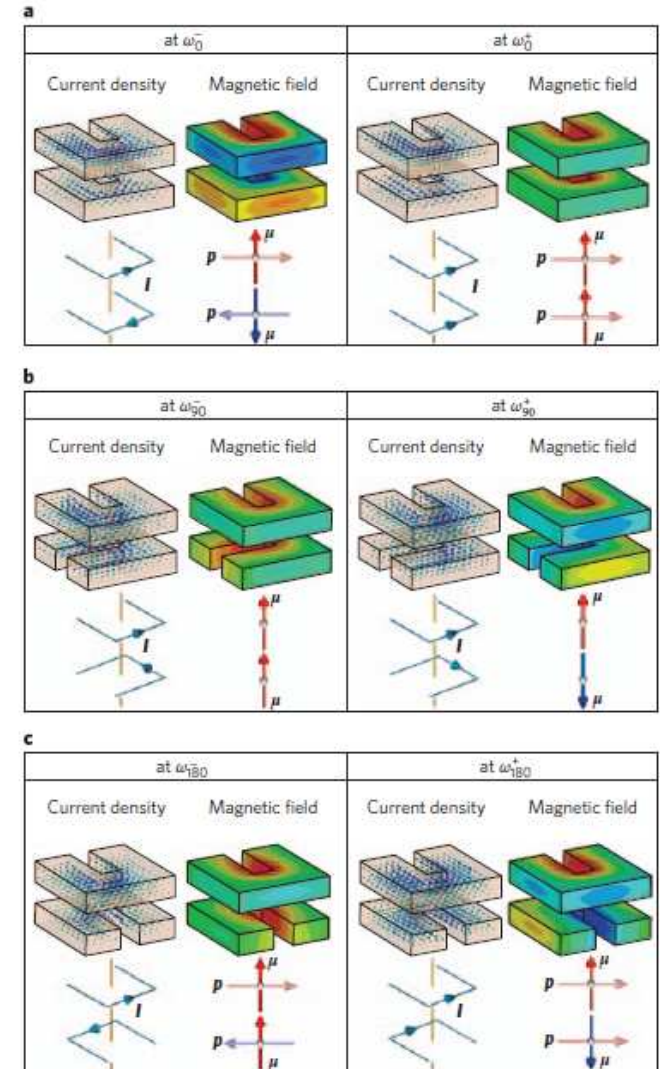
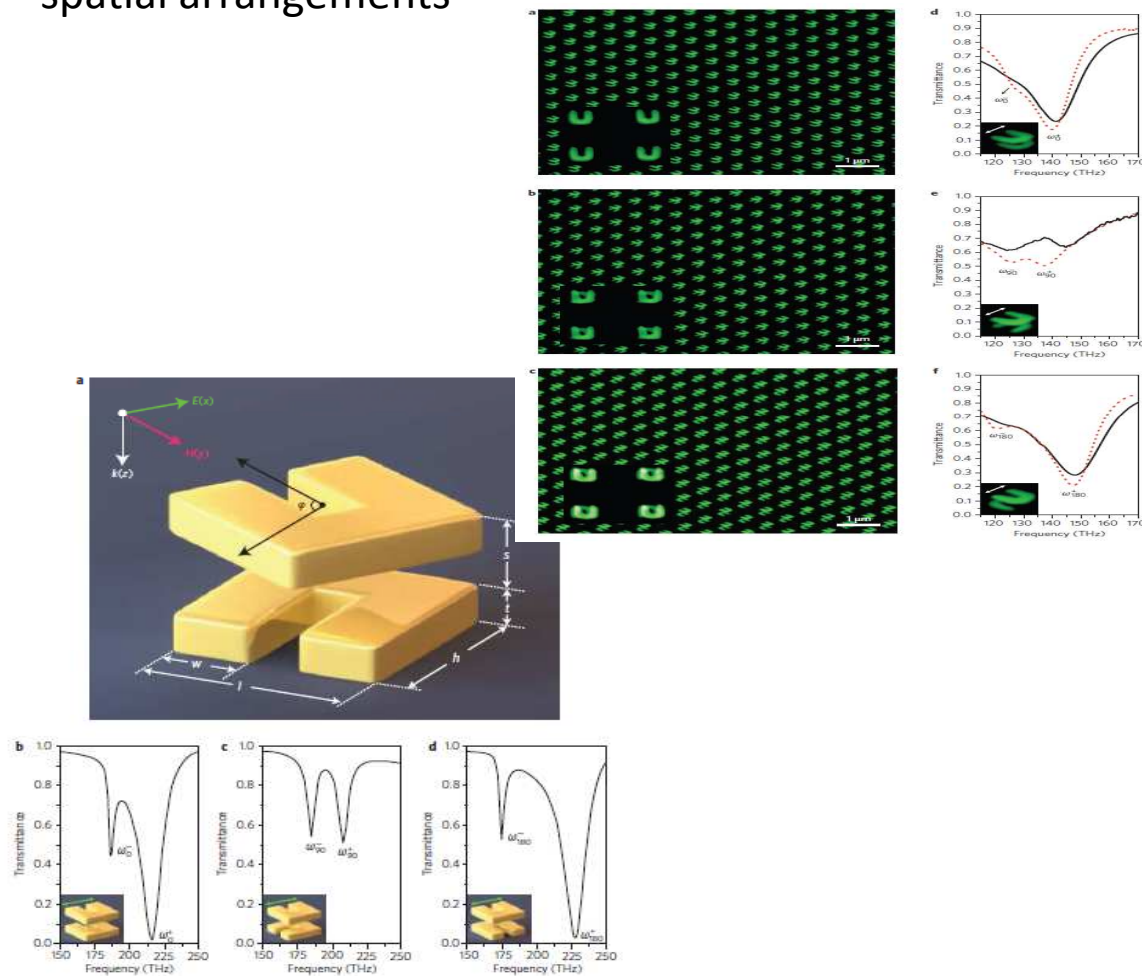
C Top view





# Stereometamaterials

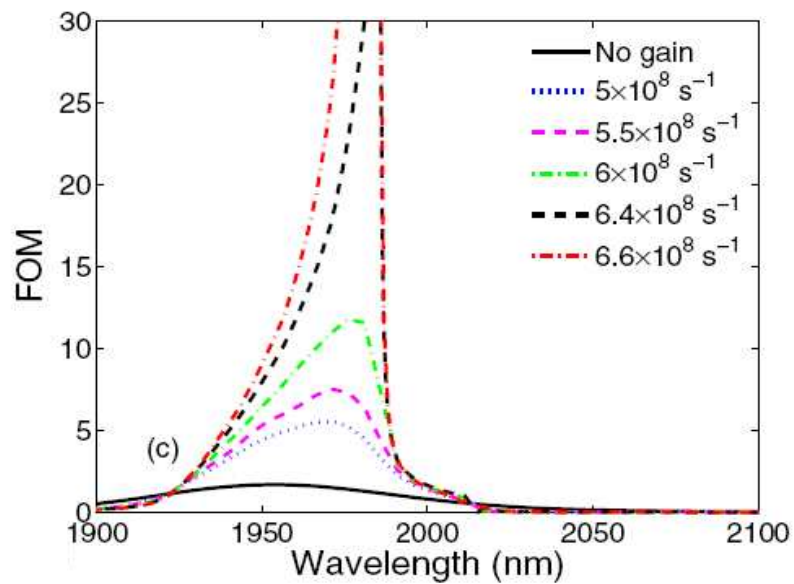
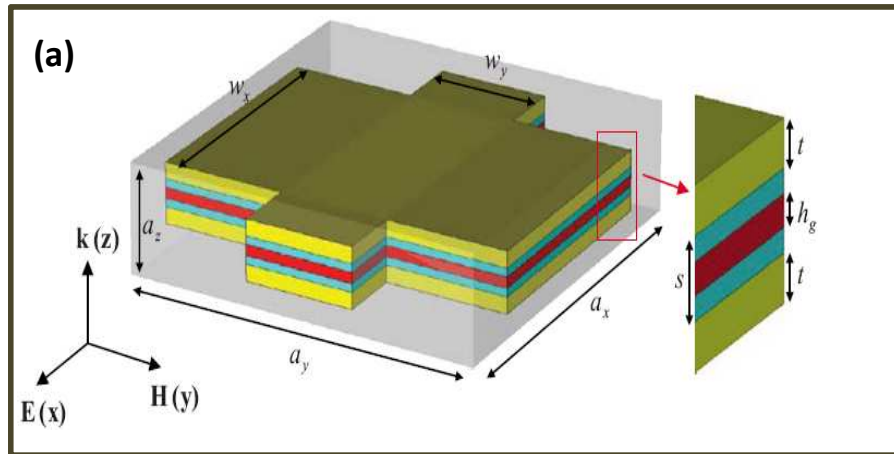
- Metamaterials with the same constituents but different spatial arrangements



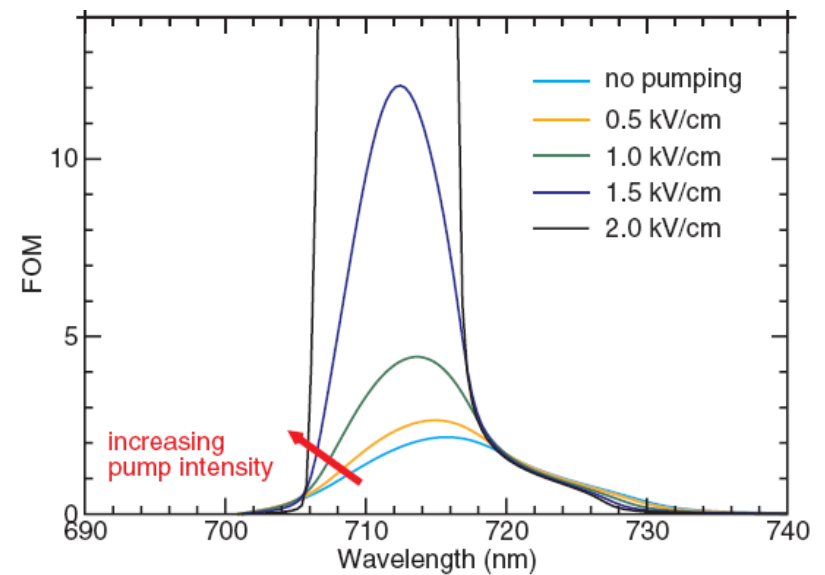
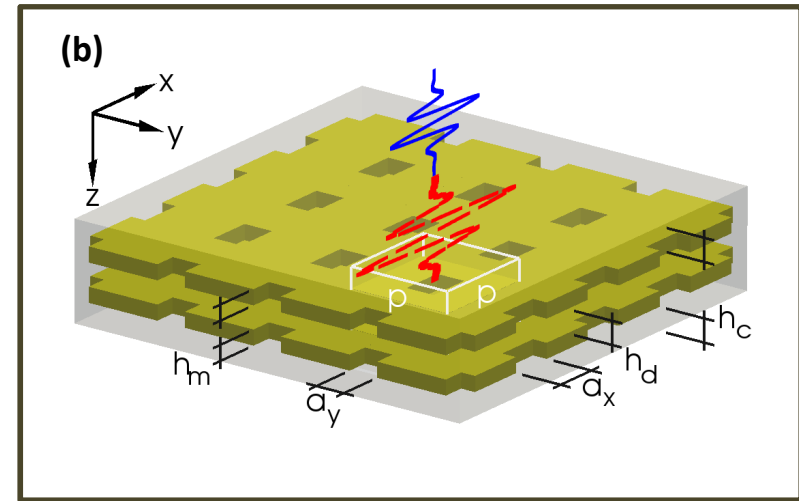
Numerical current and magnetic field distributions

# **Active Negative-Index Metamaterials**

# Active Metamaterials (3D-FDTD Simulations)



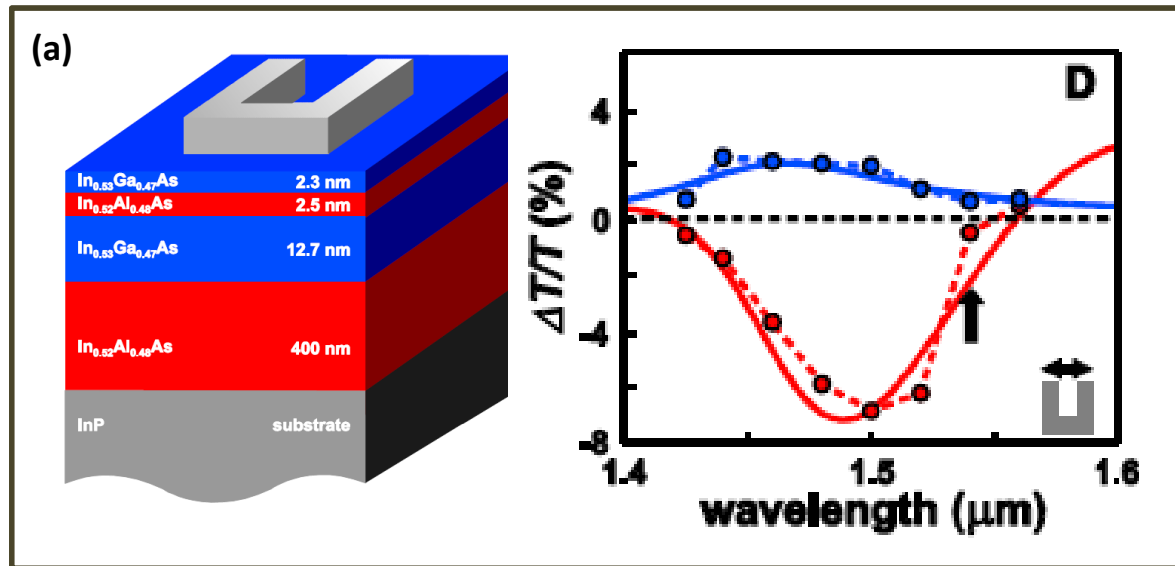
$$\text{FOM} = -n'/n''$$



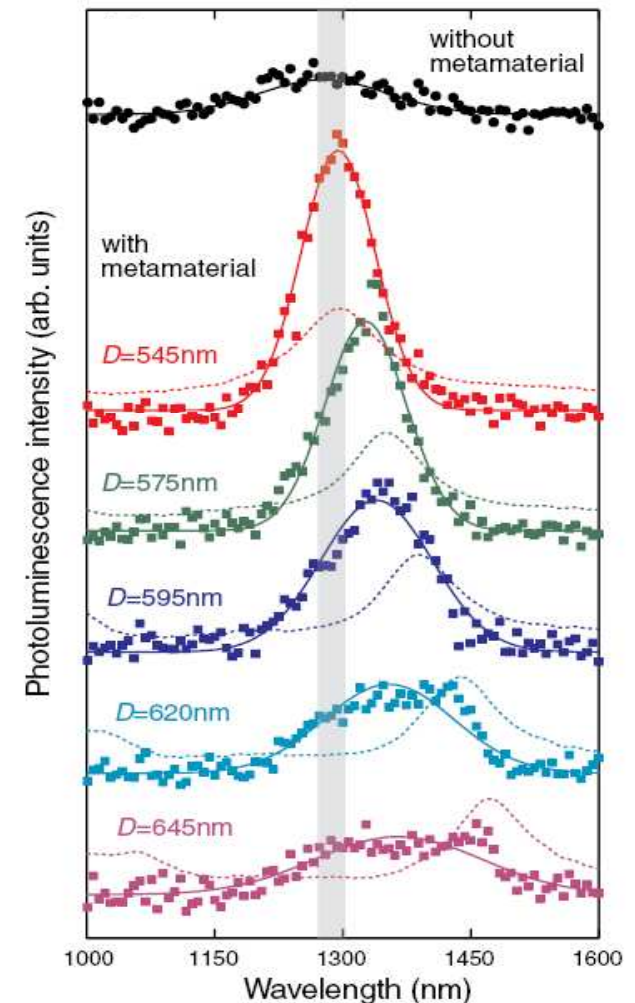
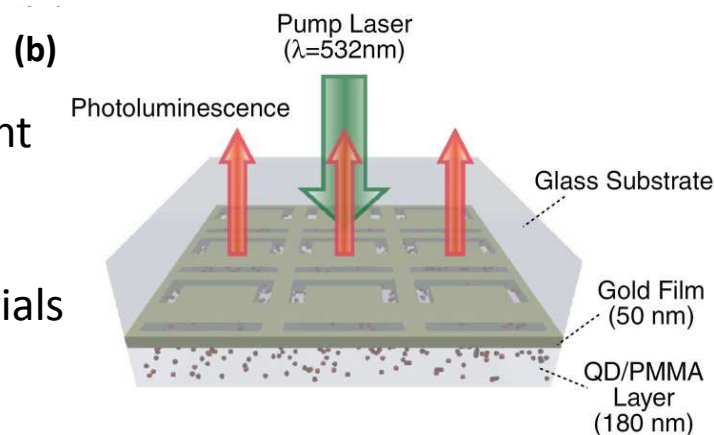
(a) Soukoulis group, PRB. 82, 121102(R), (2010)  
 (b) Ortwin Hess group, PRL. 105, 127401, (2010)

# Active Metamaterials (Experiments)

- Arrays of Ag split-ring resonators coupled to InGaAs single-quantum-well gain



- Multifold Enhancement of Quantum Dot Luminescence in Plasmonic Metamaterials

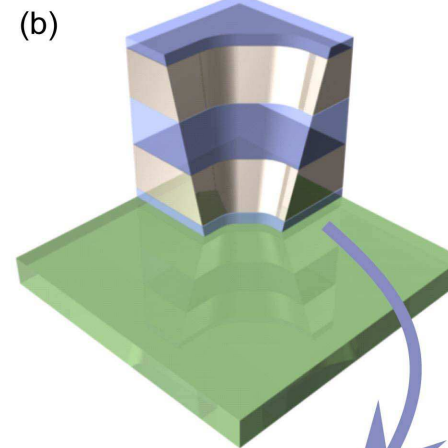
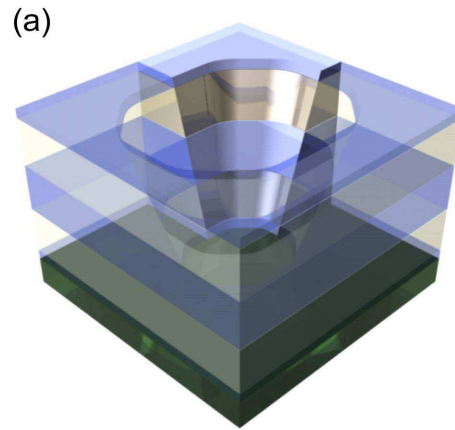


(a) Wegener group, OE. 18, 24140, (2010)

(b) Zheludev group, PRL. 105, 227403, (2010)

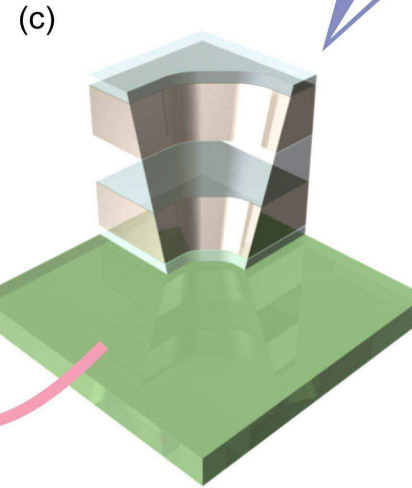
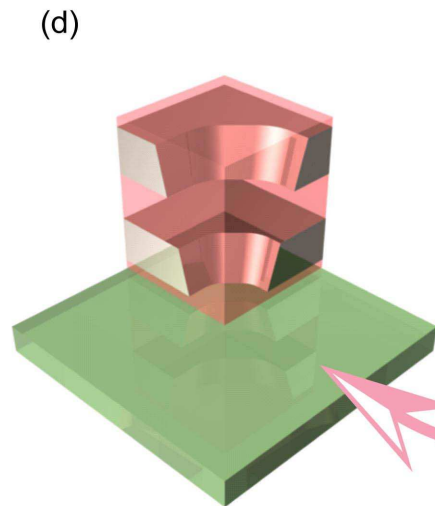
# Structure and Fabrication Process

a) Unit cell of fishnet with 50 nm alumina as spacer



b) A quarter of fishnet with an alumina spacer

d) After coating with Rh800/epoxy; structure has dye/epoxy in spacer region and atop

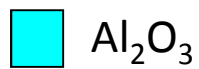
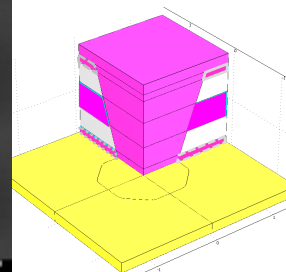
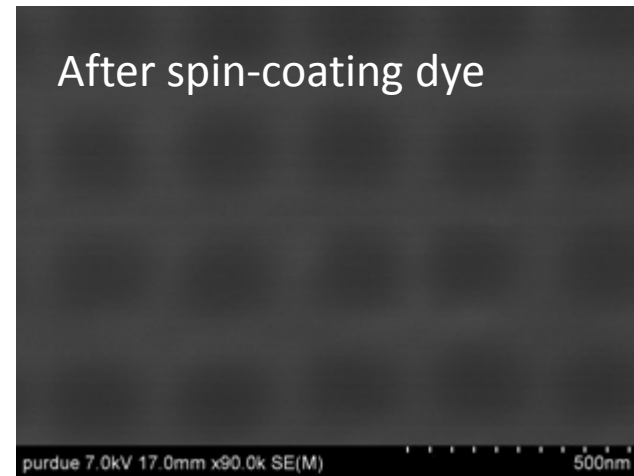
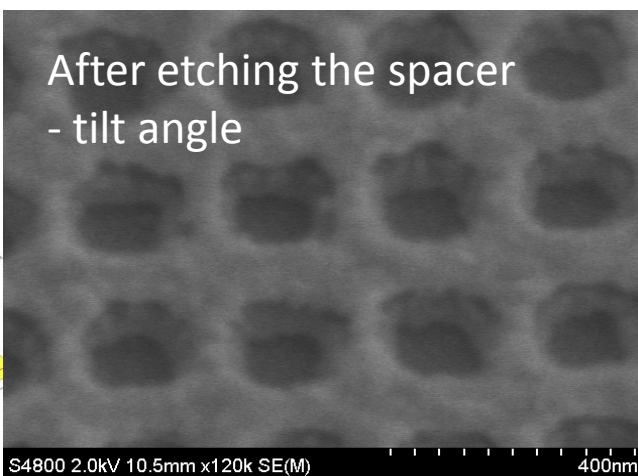
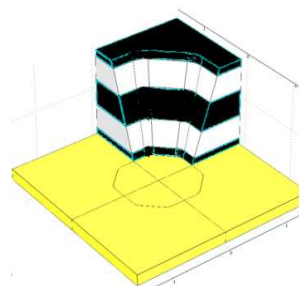
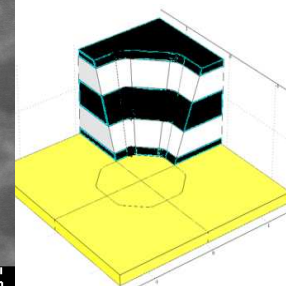
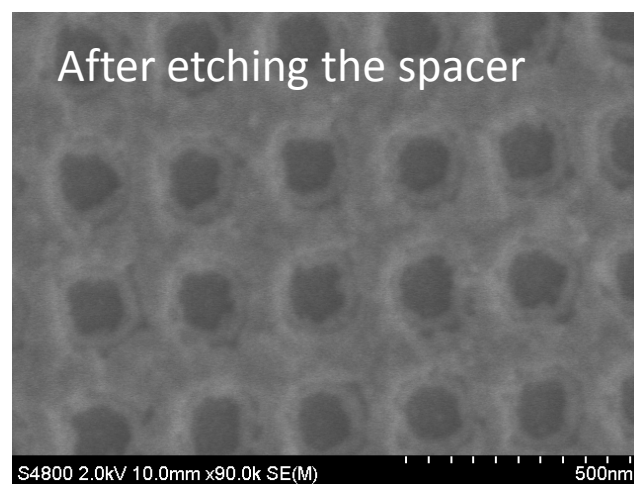
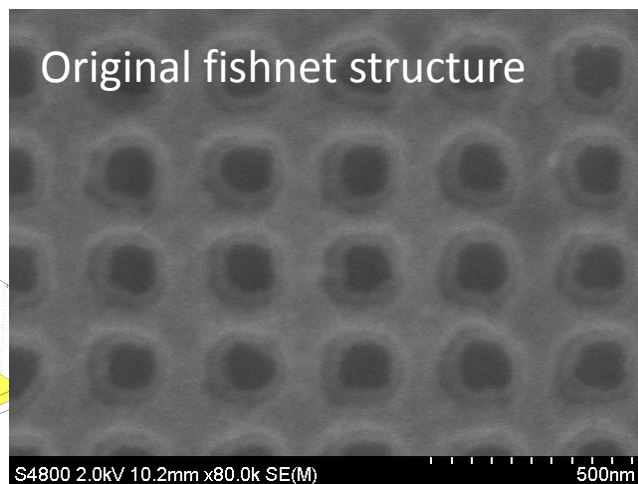
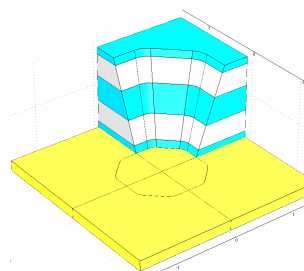


c) After etching alumina





# FESEM Images



Al<sub>2</sub>O<sub>3</sub>



Rh800/SU-8



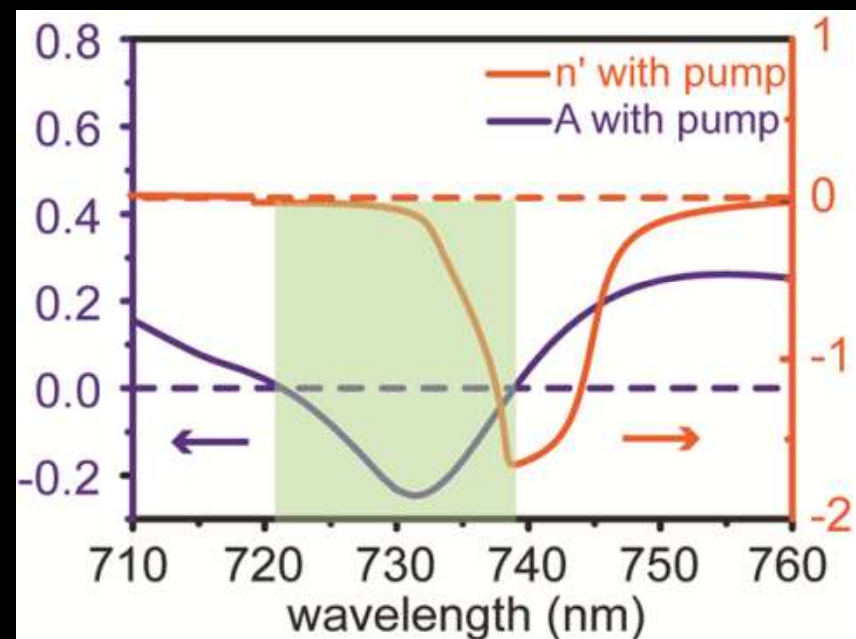
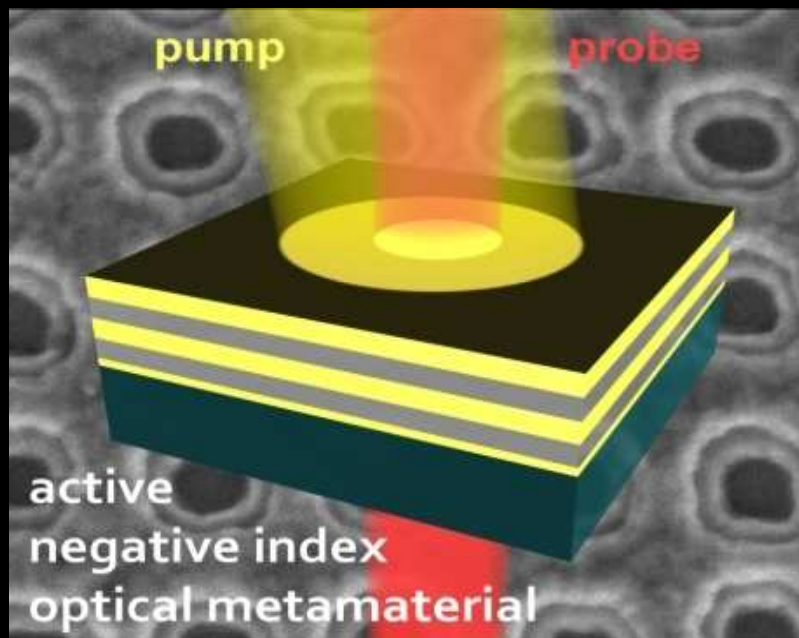
Air



Silver

# Loss Free NIM

## ■ Optical NIM with Negative Absorptance

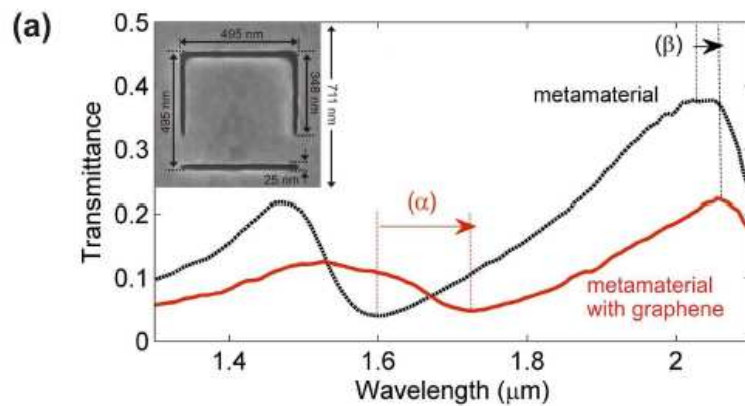
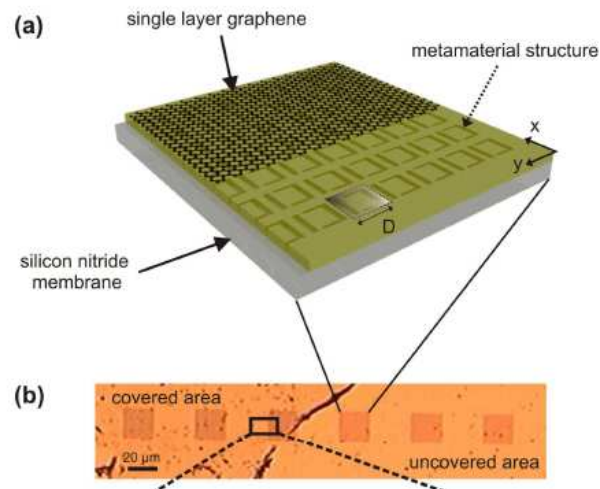


- wavelength range for negative  $n'$ : 720 nm - 760 nm
- wavelength for negative absorptance: 720 nm - 740 nm



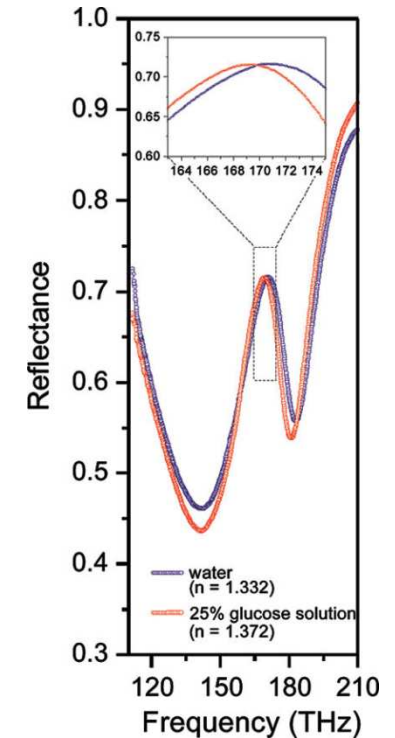
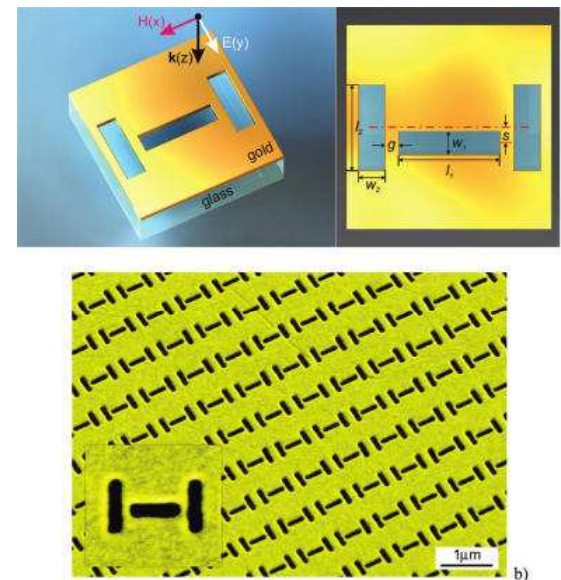
# **Metamaterials for Sensing**

# Metamaterials for Sensing



## Graphene+metamaterial for sensing

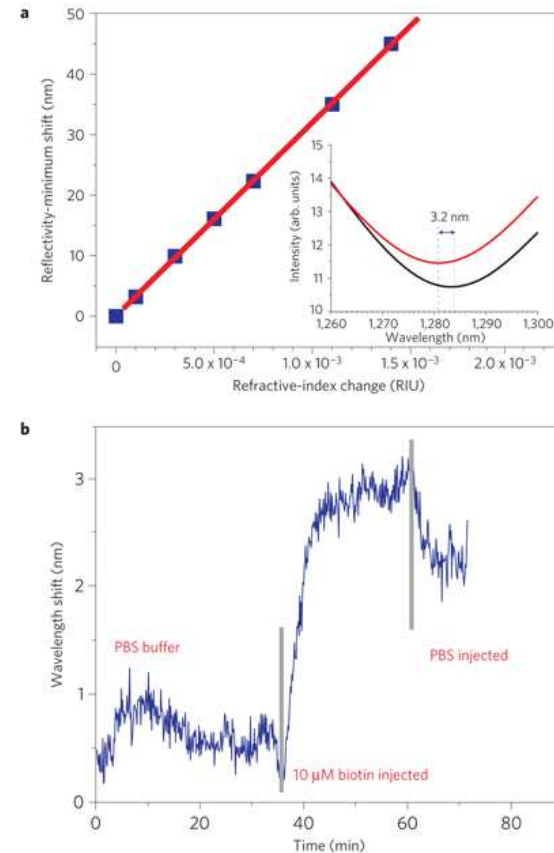
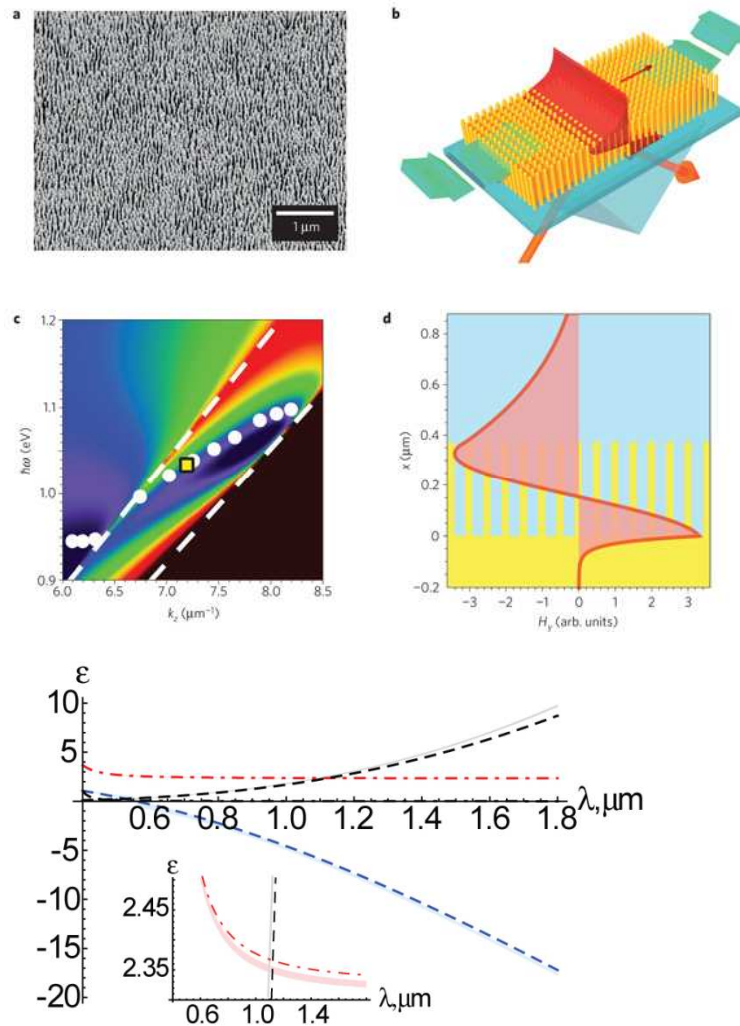
Papasimakis, et al, OE (2010) (Zheludev group)



## EIT metamaterial for sensing

N. Liu, et al, Nano. Lett.. (2010) (Gissnen group)

# Hyperbolic Metamaterials for Biosensing

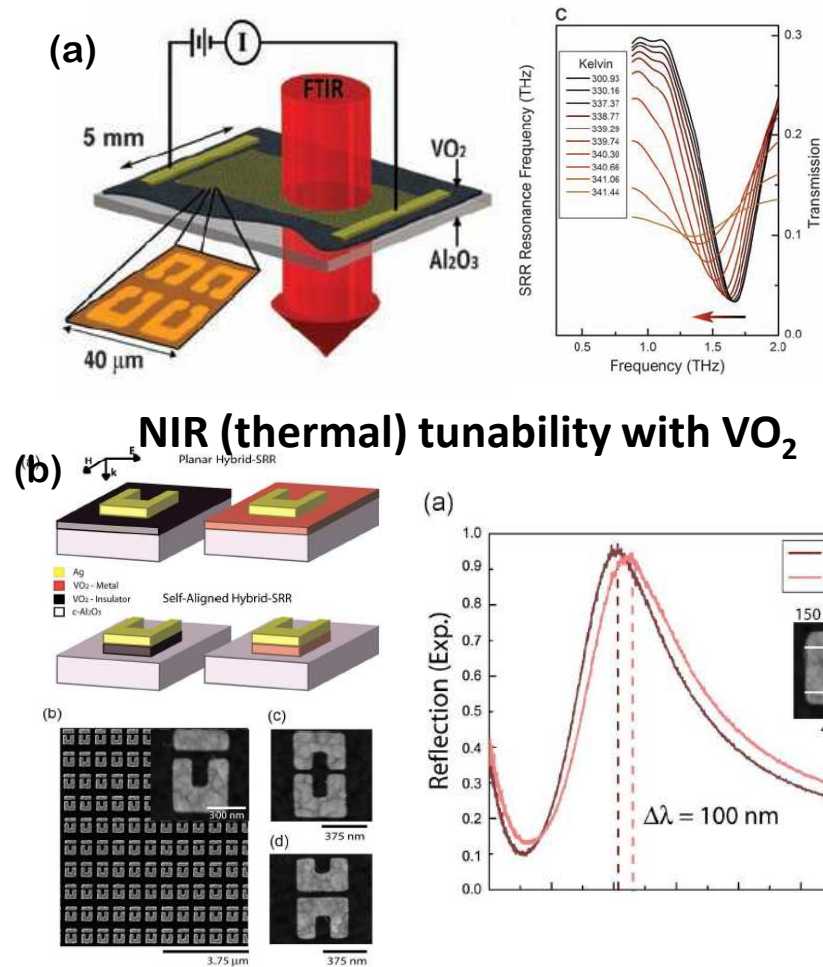


More than 100 times sensitive  
than other SPR based sensors

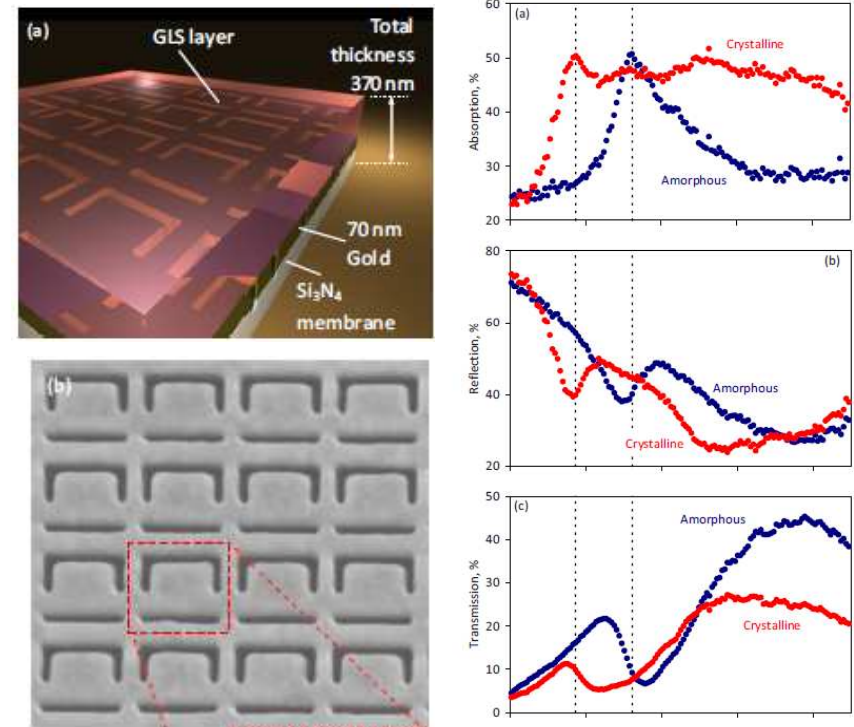
# **Tunable, Ultrafast, & Nonlinear Metamaterials**

# Tunable MMs with Phase Change Components

## Electrically controllable memory with VO<sub>2</sub>



## (c) Tunability with ChG



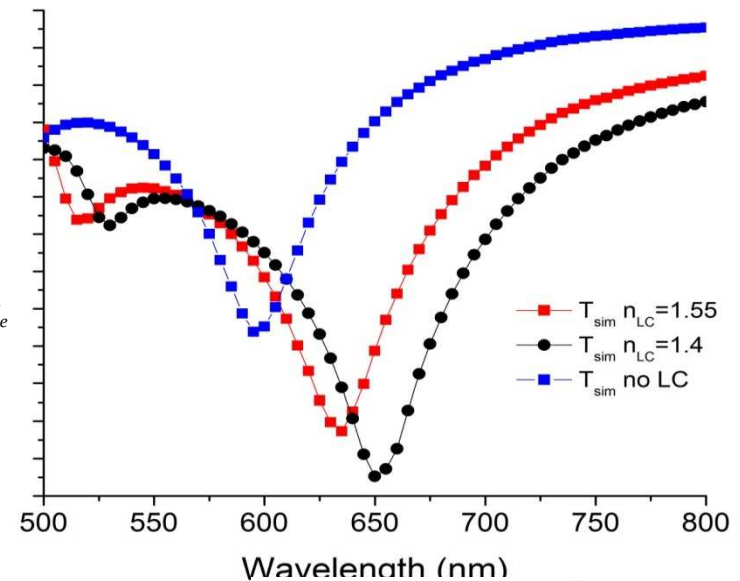
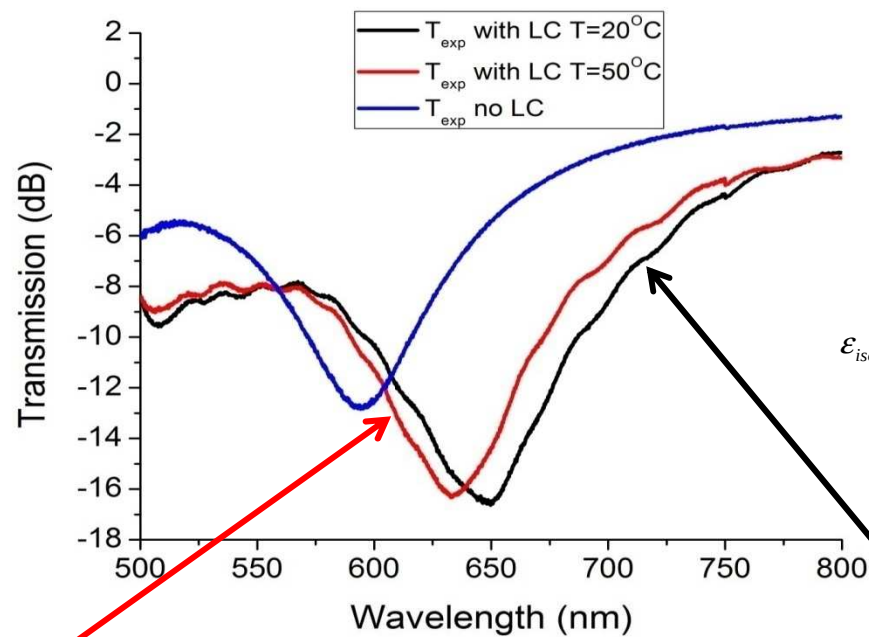
(a) T. Driscoll, et al, Science, (2009) (Smith and Basov)

(b) M. J. Dicken, et al, OE (2009) (Atwater group)

(c) Sámson, et al, APL, (2010) (Zheludev group)

THz range – Willie Padilla

# Tunable Metamaterials



(Isotropic)

$$n_{\text{iso}}^2 = \frac{2}{3}n_o^2 + \frac{1}{2}n_e^2$$

Phase transition

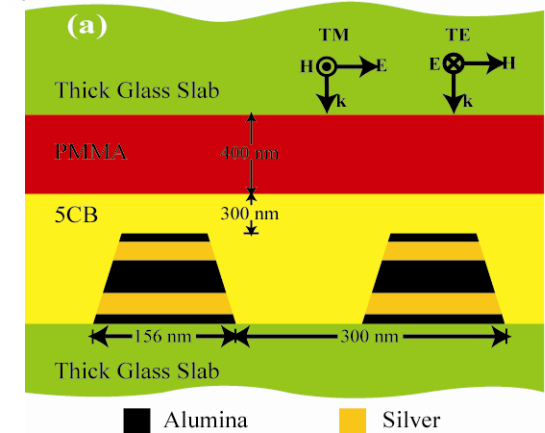
$$\Delta n = 0.17$$

$$T > T_e$$



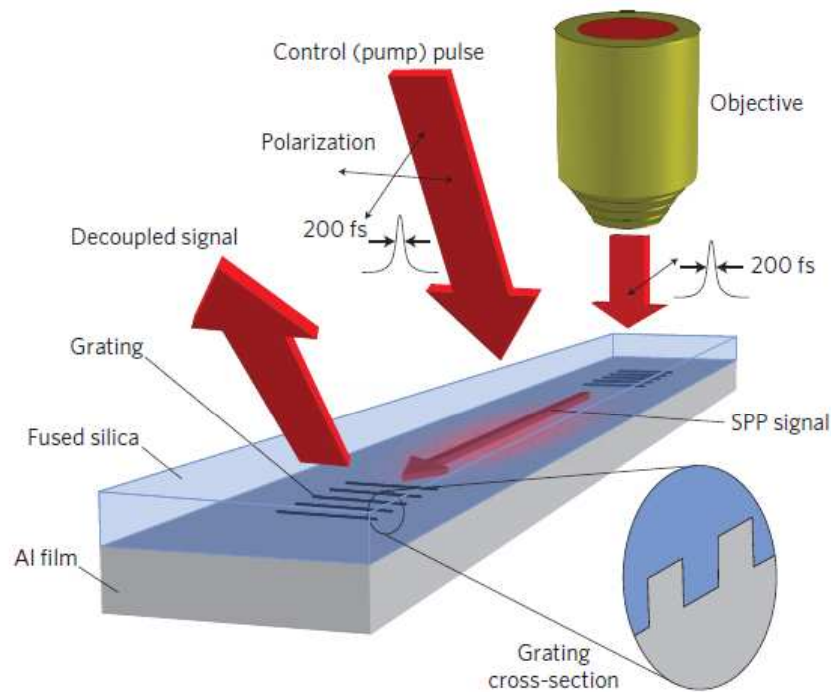
(Nematic)

$$n_{\text{eff}} = n_e$$

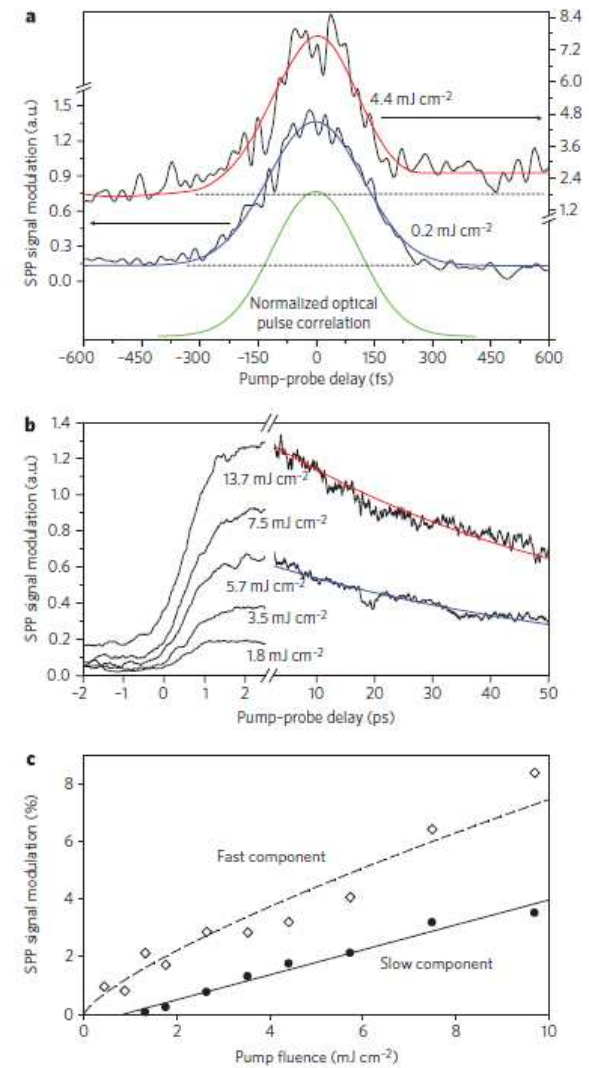




# Ultrafast Active Plasmonics

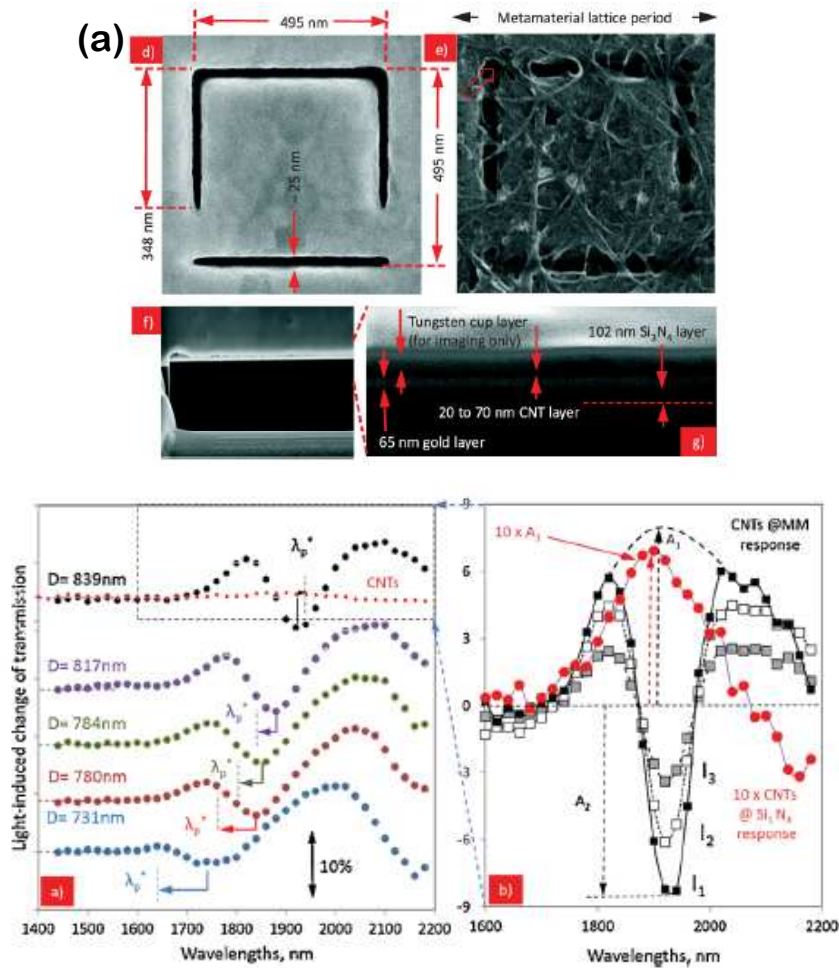


- SPP propagation influenced by optical pump
- Sub-ps control on SPPs

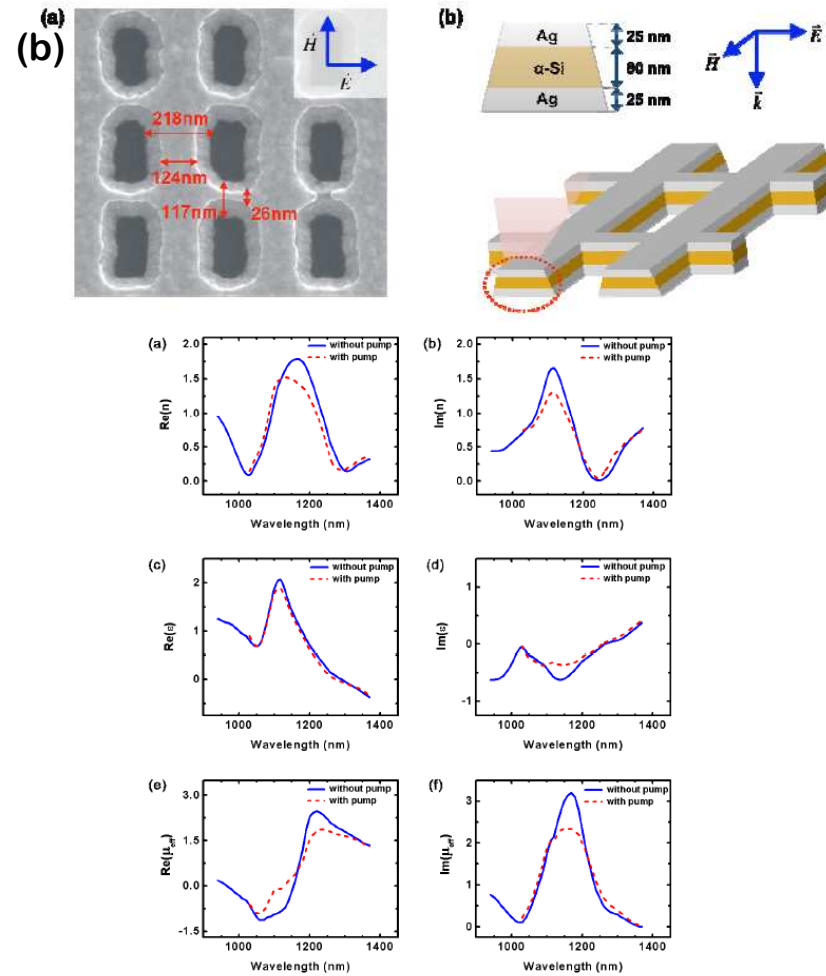


# Nonlinear Materials + Metamaterials

## Carbon nanotubes + MM



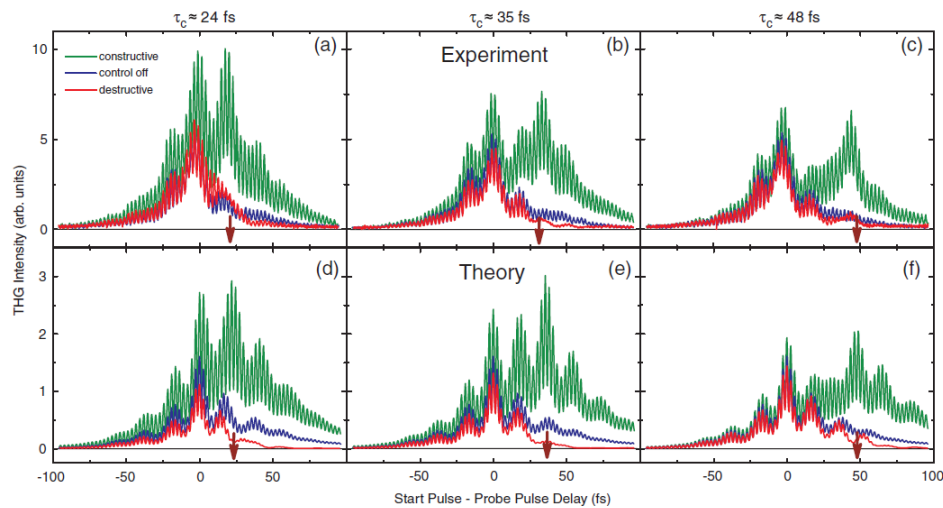
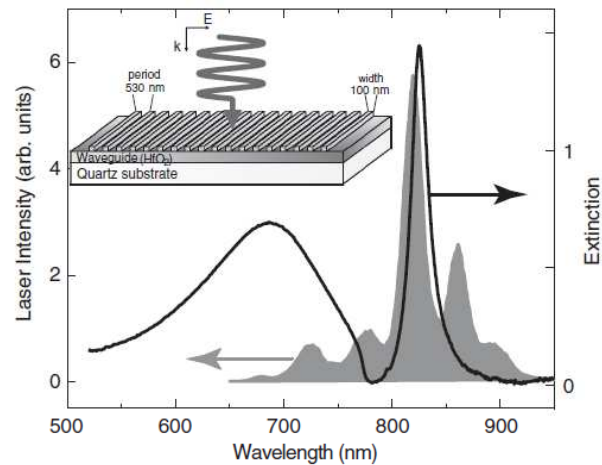
## $\alpha$ -Si+ MM



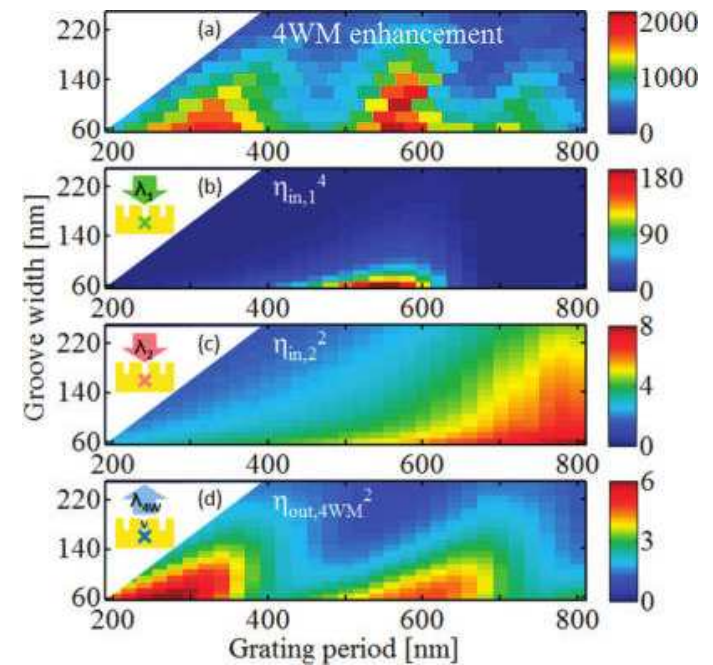
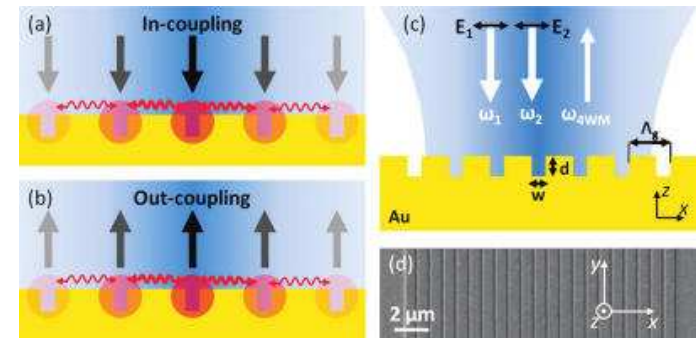
(a) Papasimakis, et al, PRL (2010) (Zheludev group)

(b) D. J. Cho, et al, OE (2009) (Bratkovsky-Zhang-Shen groups)

# Four-Wave Mixing in Metamaterials



T. Utikal, et al, PRL (2010) (Giessen group)



P. Genevet, et. al., NL (2010) (Capasso group)

# **Quantum Optics with Metamaterials: Engineering Photonic Density of States with Metamaterials**

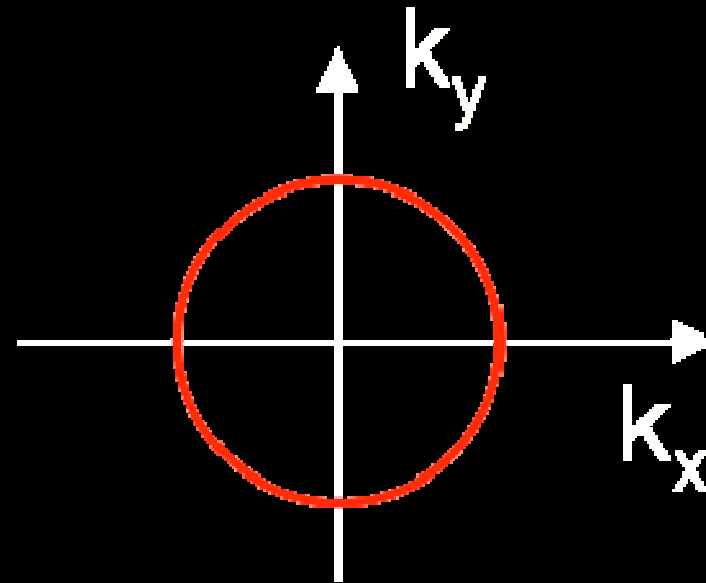
Z. Jacob, J.-Y. Kim, G. V. Naik,  
A. Boltasseva, E. E. Narimanov and V. M. Shalaev  
(Applied Physics B Centennial Volume July , 2010)

Other interesting work on Quantum Optics in MMs:  
Nordlander, J.G. de Abajo, Leonhard, O'Brien, Capasso,...

# Hyperbolic Dispersion

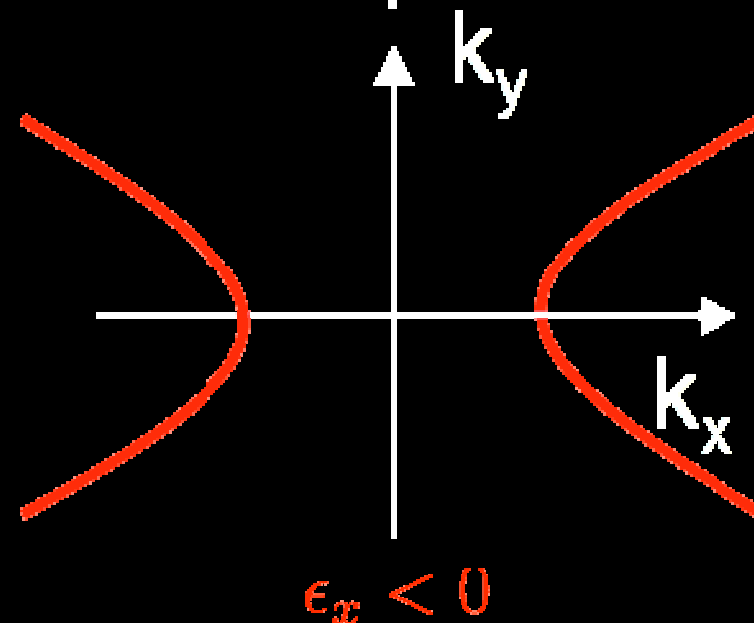
“Regular” dielectric

$$\frac{k_x^2}{\epsilon_y} + \frac{k_y^2}{\epsilon_x} = \frac{\omega^2}{c^2}$$



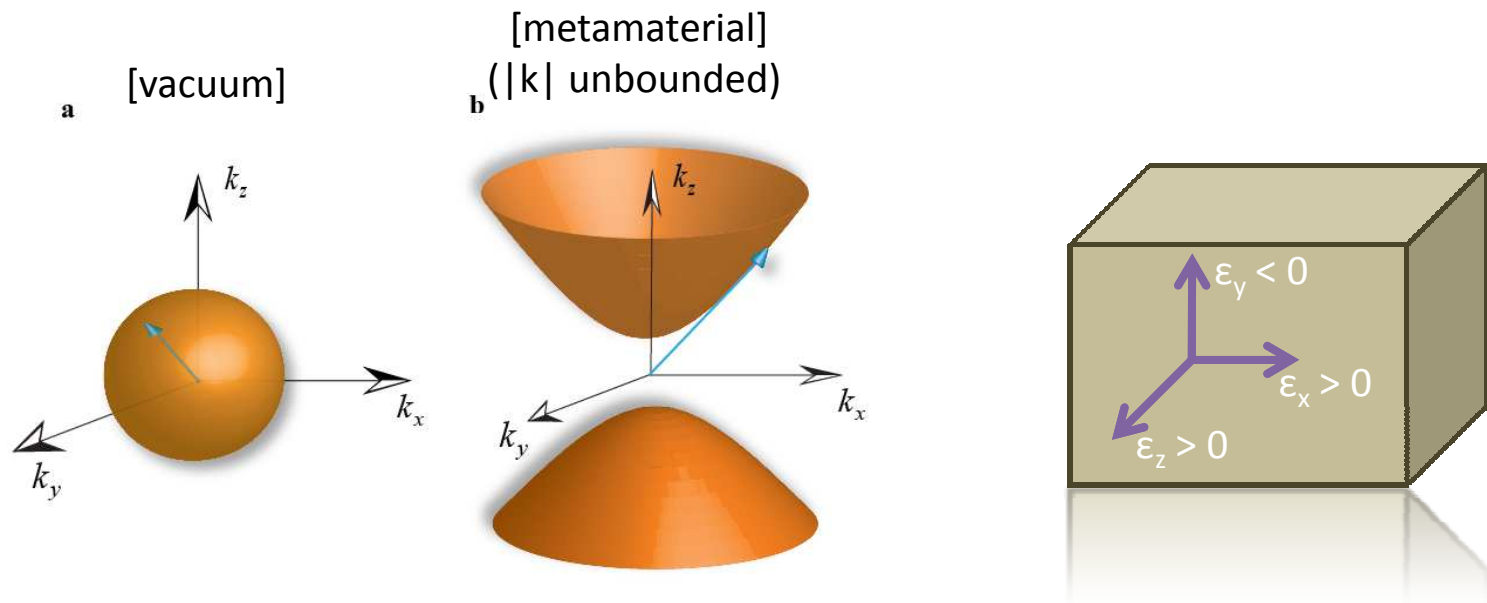
“Strongly Anisotropic” media

$$\frac{k_x^2}{\epsilon_y} + \frac{k_y^2}{\epsilon_x} = \frac{\omega^2}{c^2}$$



Special case of “Indefinite Media”, D.Smith et al, 2003

# PDOS in Hyperbolic Metamaterial?

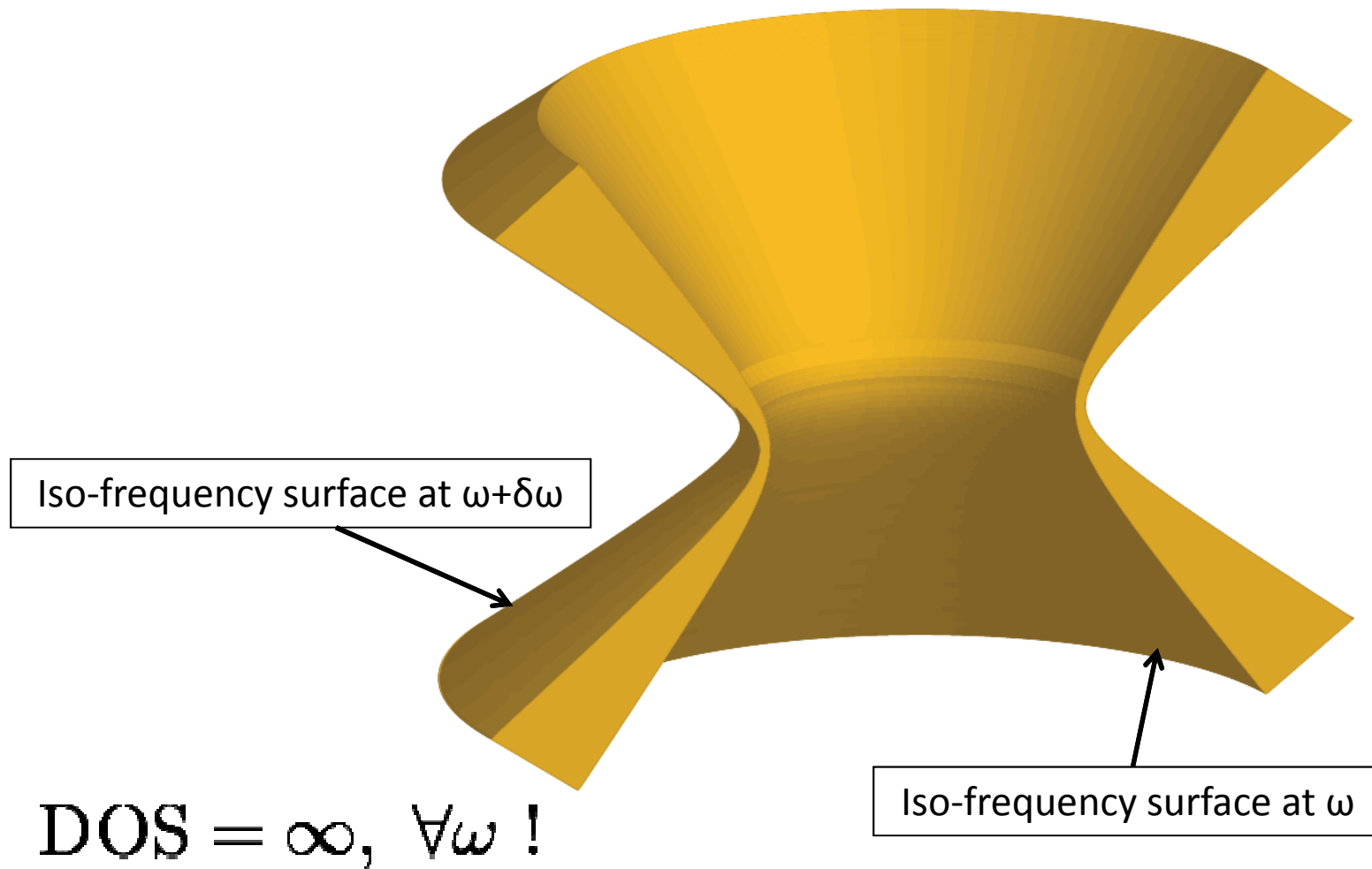


**Singularity in density of states!!!!**

- Hyperbolic dispersion supports high spatial wavevectors compared to vacuum
- Large contribution to DOS from the “high  $k$ ” states (think beyond imaging!)

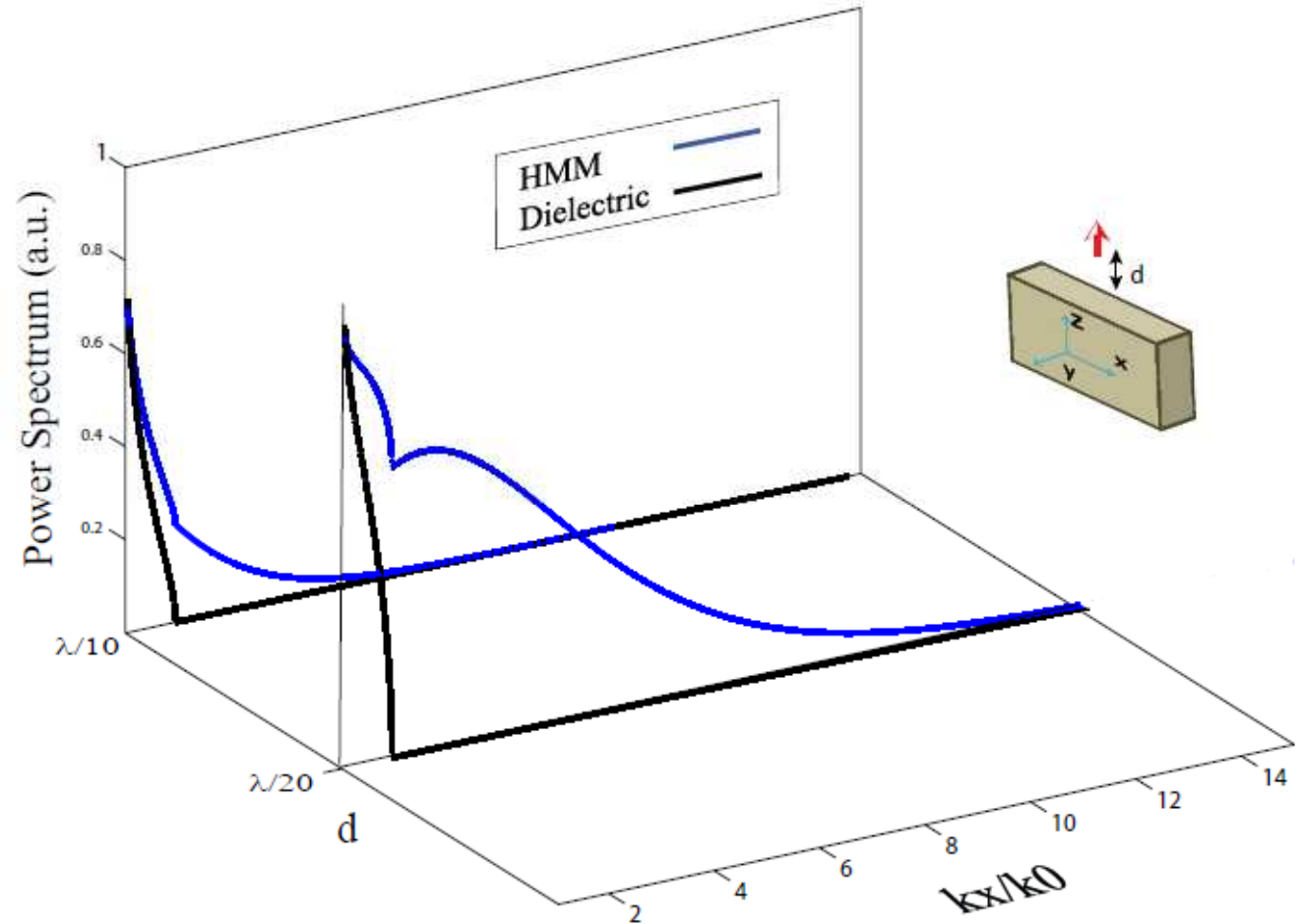
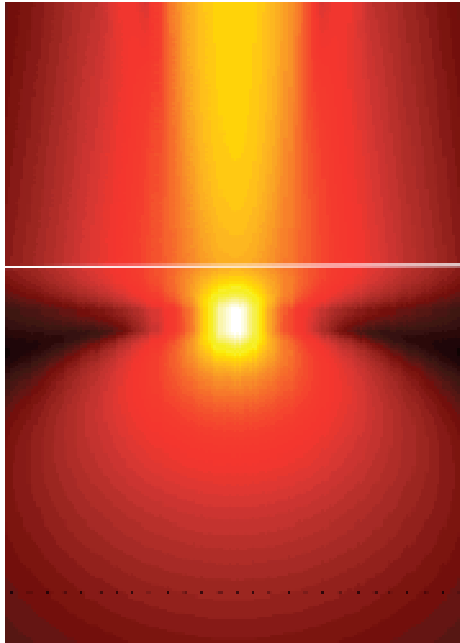


# Photonic Density of States (PDOS)



Broadband Purcell effect: Radiative decay engineering with metamaterials  
- Z. Jacob, I. Smolyaninov, E. Narimanov (*on Arxiv*)

# Emission Power Spectrum



Calculation Methods:  $\Gamma = \frac{P}{\hbar\omega}$  : Ford and Weber (1984)  
QED: Hughes group (2009)

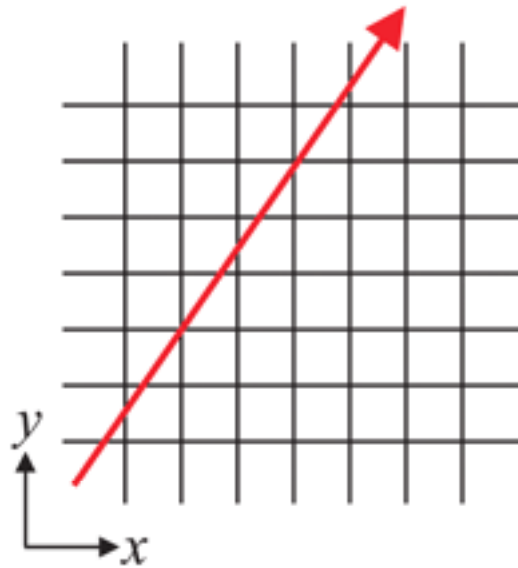
Experiment: Z. Jacob ,et al, Appl. Phys. B (2010)

# **Transformation Optics: Optical Cloaking, Trapped Rainbow, & Maxwell Fish-eye and Eaton Lenses**

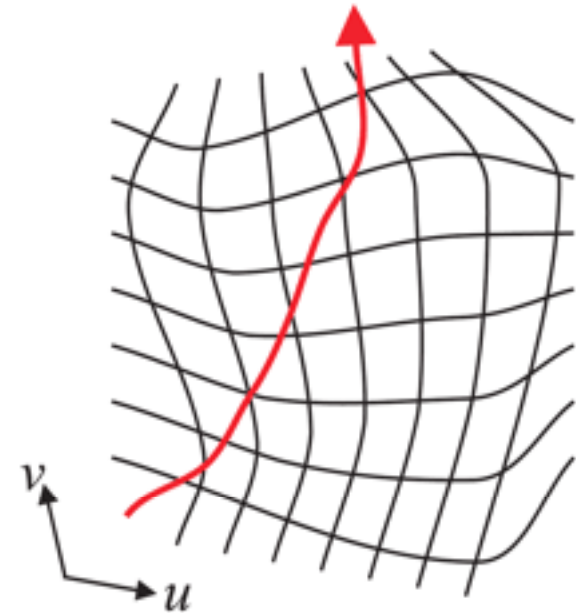
V. M. Shalaev, Transforming Light, Science, Oct. 17, 2008

# Designing Space for Light with Transformation Optics

**Fermat:**  
 $\delta \int n dl = 0$   
 $n = \sqrt{\epsilon(r)\mu(r)}$   
  
“curving”  
optical space



Straight field line  
in Cartesian coordinate



Distorted field line  
in distorted coordinate

- Spatial profile of  $\epsilon$  &  $\mu$  tensors determines the distortion of coordinates
- Seeking for profile of  $\epsilon$  &  $\mu$  to make light avoid particular region in space — optical cloaking

David A.B. Miller: Cloaking with “active sources”

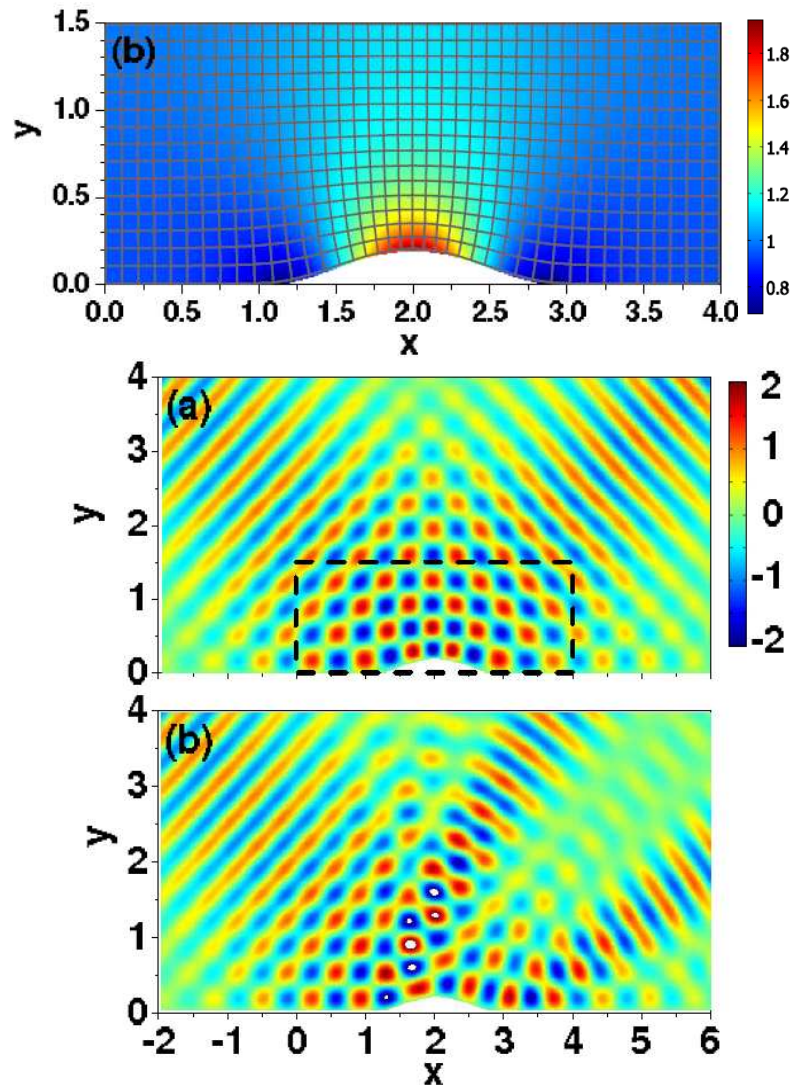
Pendry et al., Science, 2006

Leonhard, Science, 2006

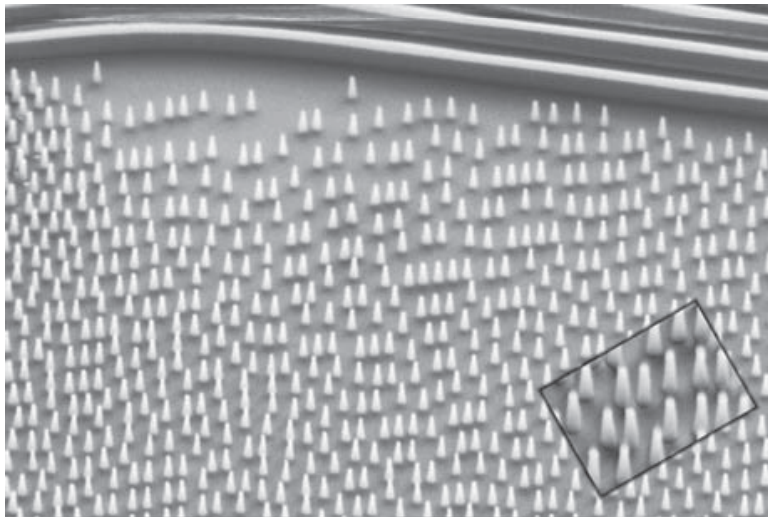
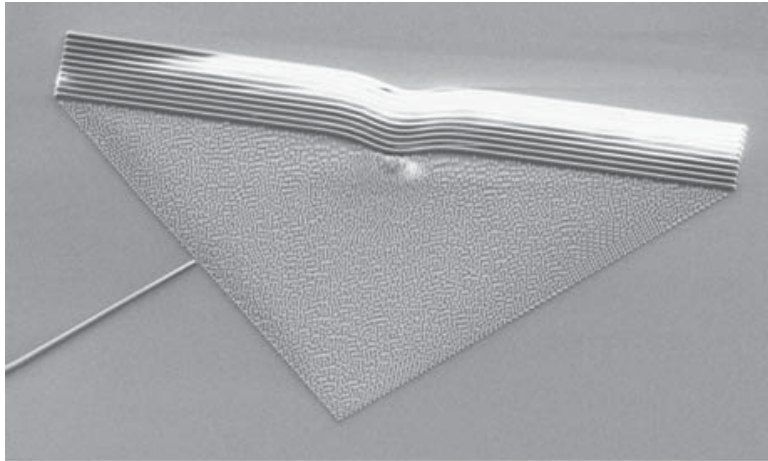
Greenleaf et al (2003)

L. S. Dolin, Izv. VUZ, 1961

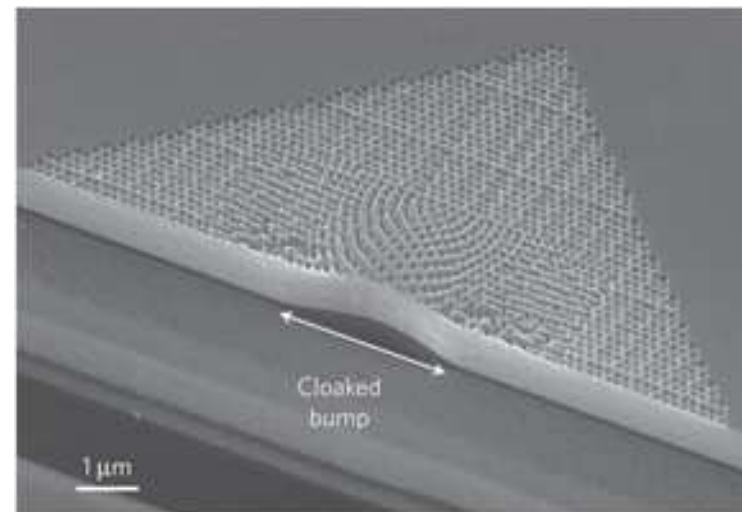
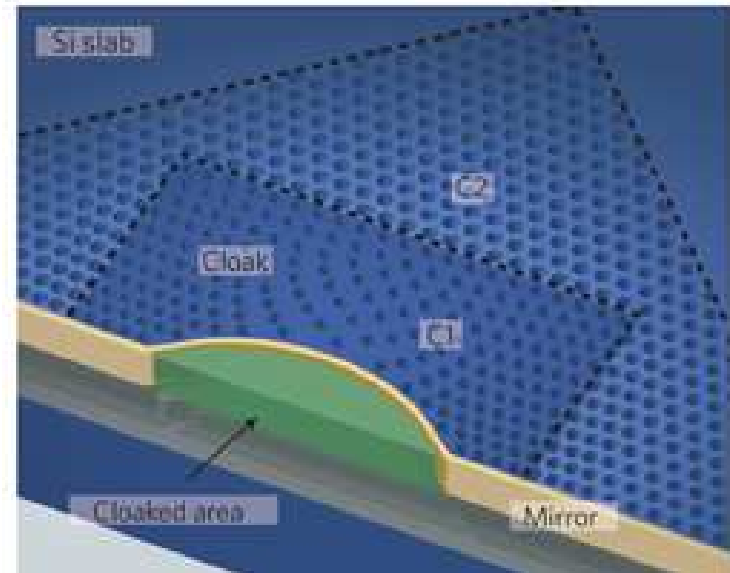
# Invisible Carpet (ground-plane cloak)



picture from discovery.com

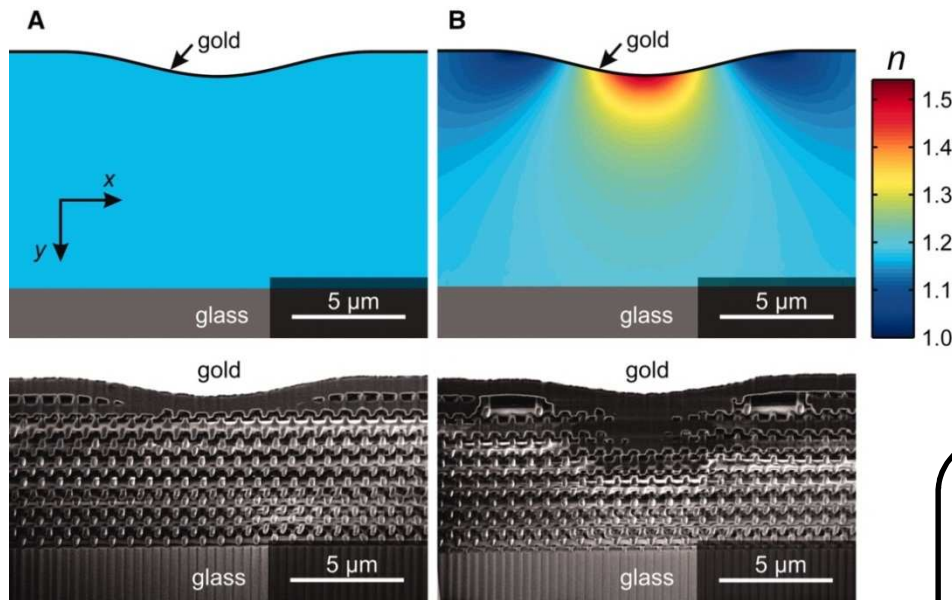


L. H. Gabrielli, *et al.*, *Nat. Photonics* **3**, p.461, Aug 2009.  
(M. Lipson group)

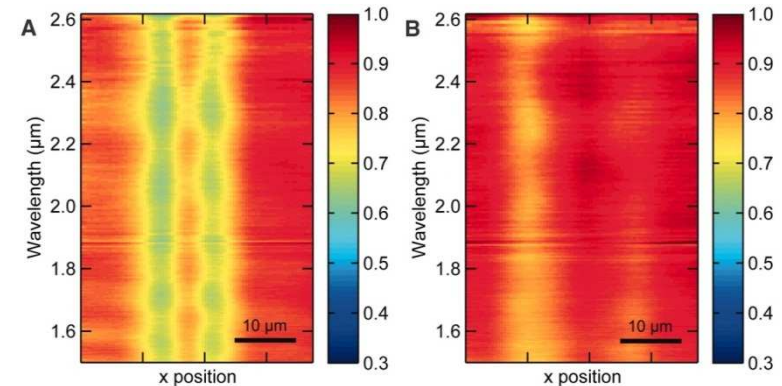


J. Valentine, *et al.*, *Nat. Mater.* **8**, p.568, Jul 2009.  
(X. Zhang group)

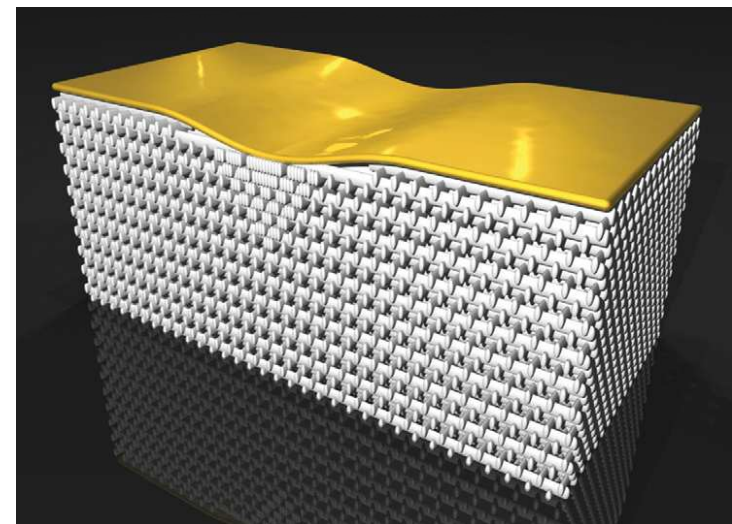




Target refractive index ( $n$ ) distributions (top) and oblique-view electron micrographs of fabricated structures after FIB milling (bottom). (A) A bump without a cloak. (B) A bump with a cloak.

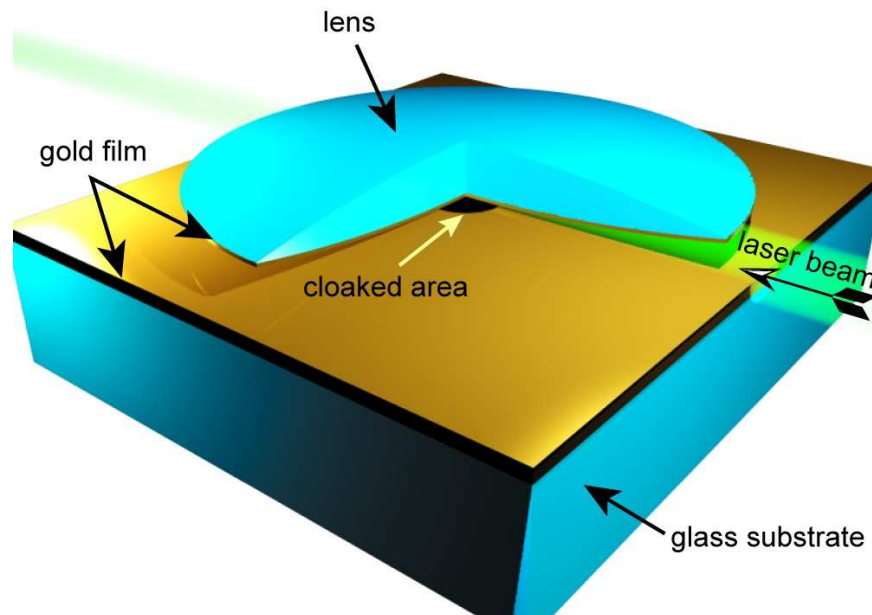


Optical characterization of the 3D structures with **unpolarized** light in bright-field mode. (A) A bump without a cloak. The bump is immediately visible. (B) (B) Result for a bump with a cloak that approaches the expectation for an ideal cloak (constant intensity).



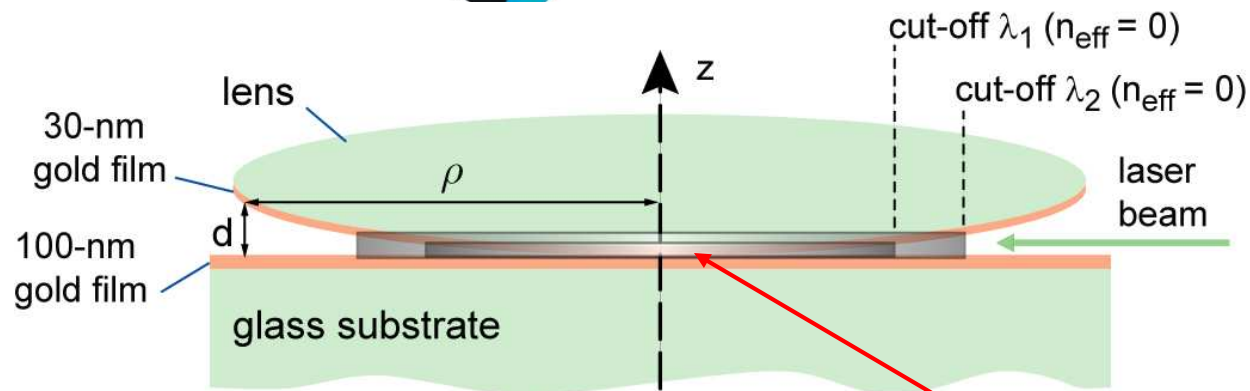
Blueprint of the 3D carpet-cloak structure

# Broadband Optical Cloak in Tapered Waveguide



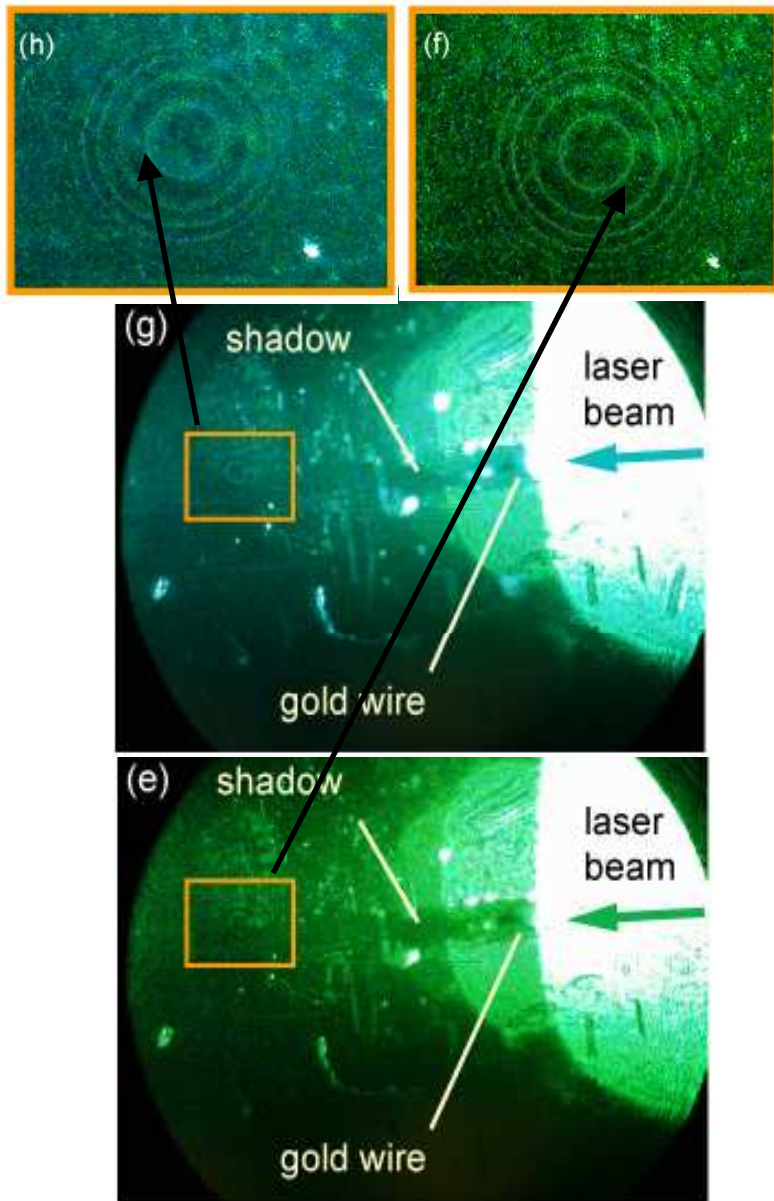
$$\begin{aligned} \left(\omega/c\right)^2 &= k_\rho^2 + \left(m/\rho\right)^2 + \left[\pi l/d(\rho)\right]^2 \\ &= k_\rho^2 + k_\phi^2(\rho - b)^{-2} \end{aligned}$$

Z. Jacob and E. E. Narimanov, *OE*, 2008.



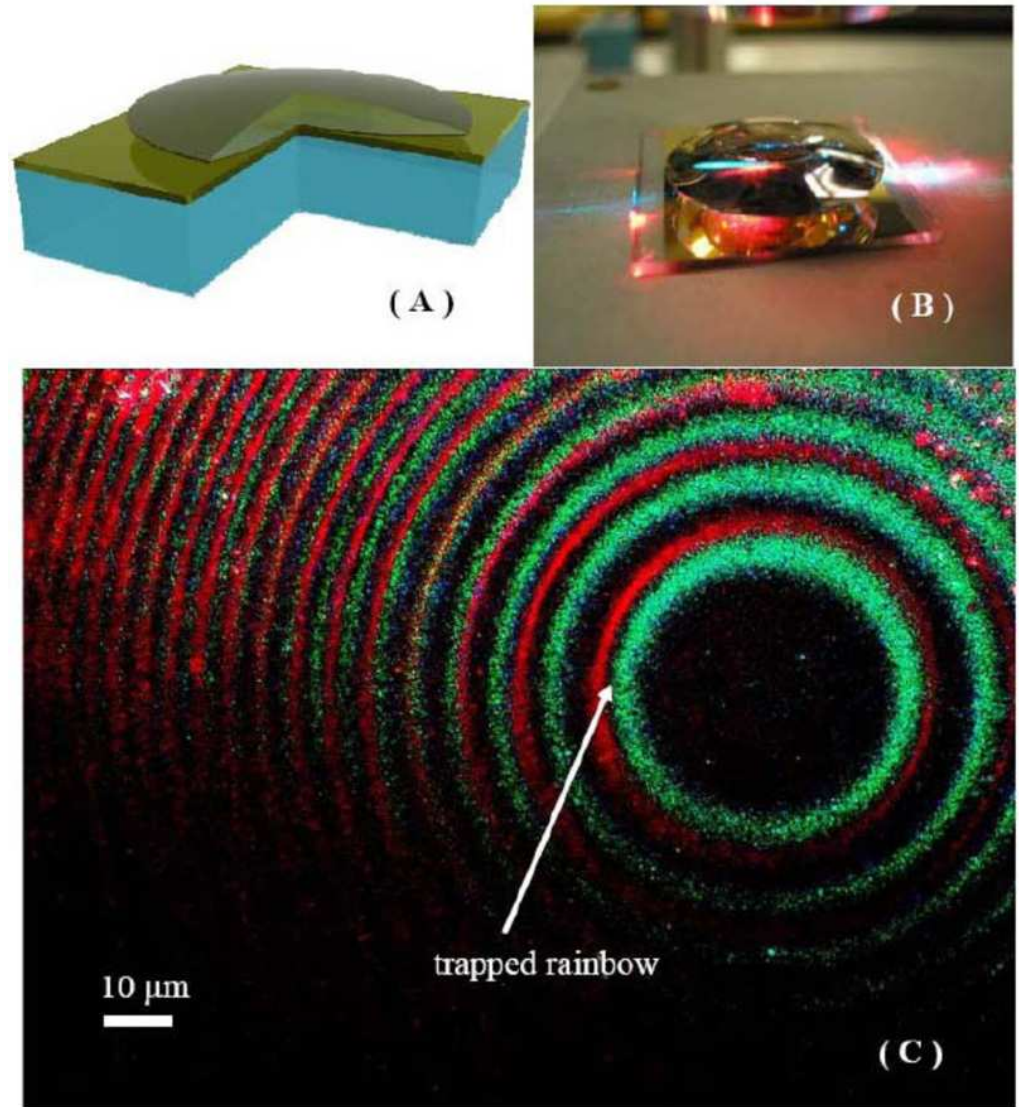
***Cloaked area***

I. I. Smolyaninov, et al, *PRL*, 2009.



I. I. Smolyaninov, et al, *PRL*, 2009.

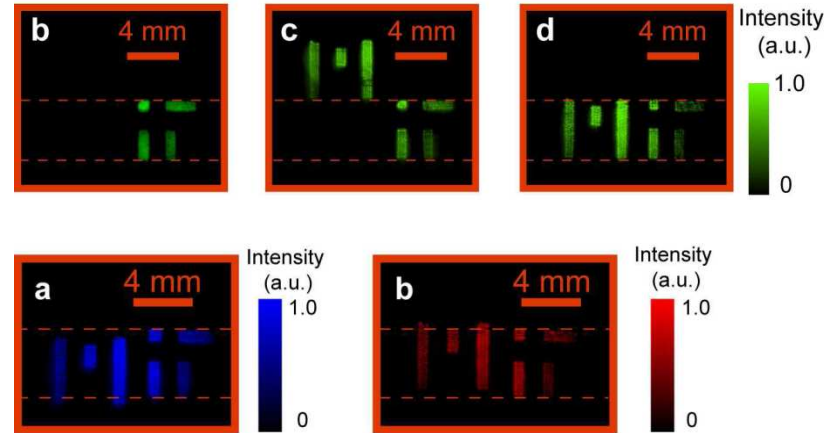
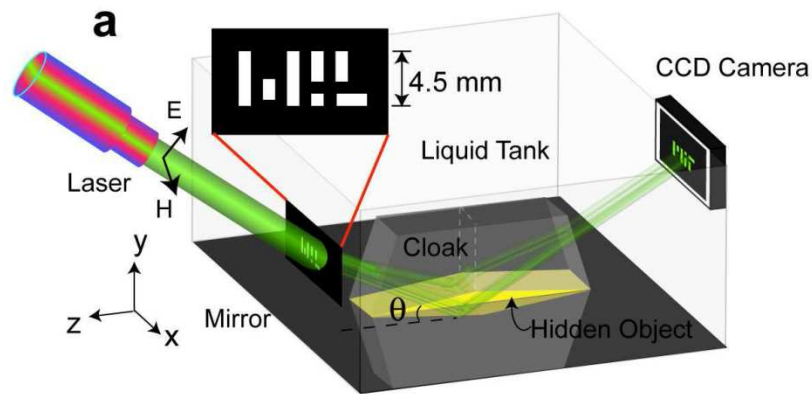
## Optical Cloak & Trapped Rainbow



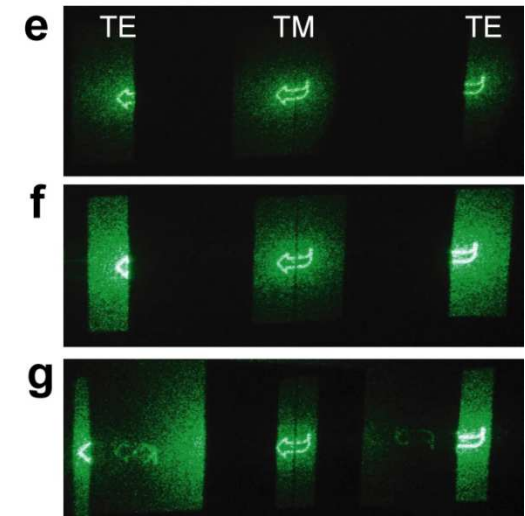
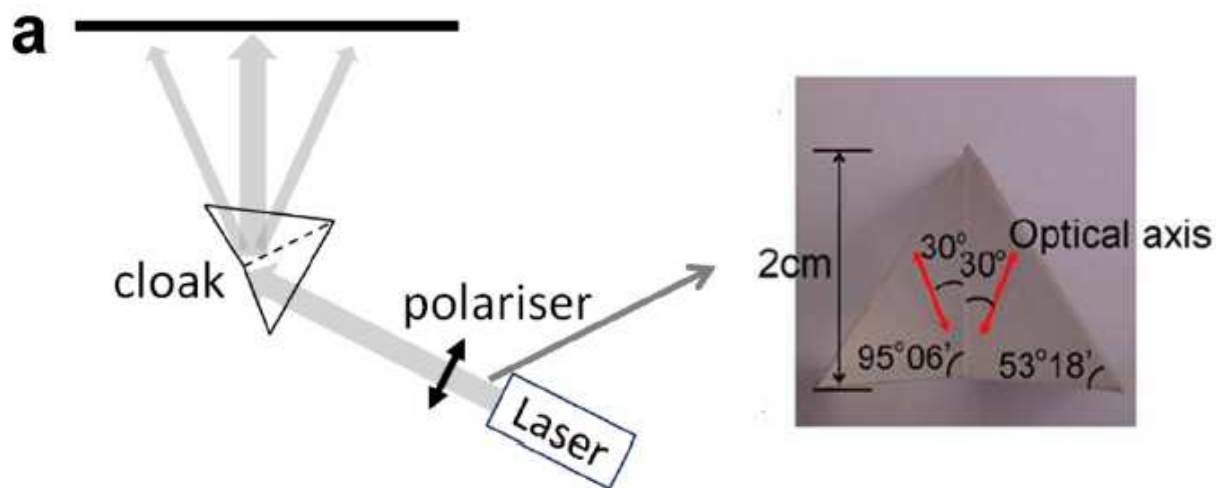
V. N. Smolyaninova, et al, *APL*, May 24 2010.



# Macroscopic Cloaking Based on Calcite

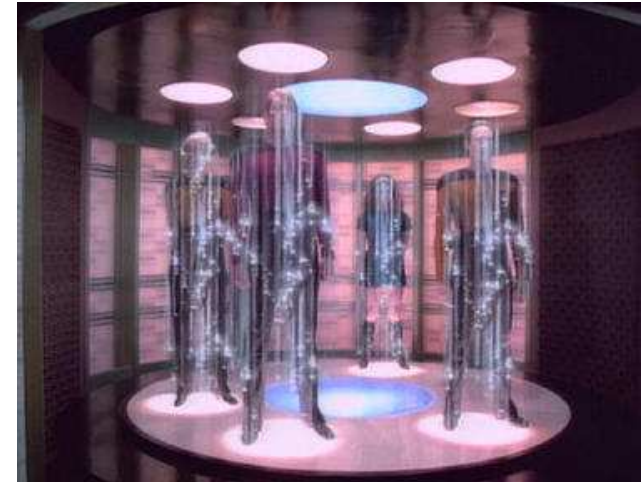
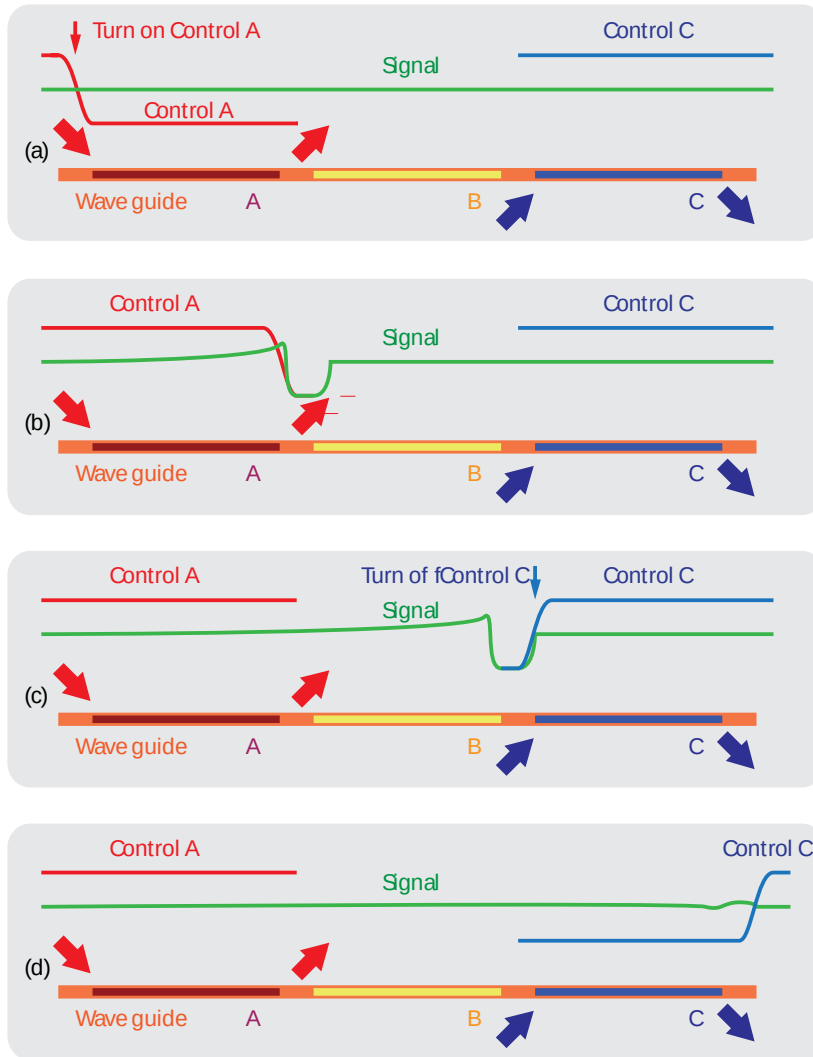


B. Zhang, et al, [arXiv:1012.2238](https://arxiv.org/abs/1012.2238) (Singapore-MIT)

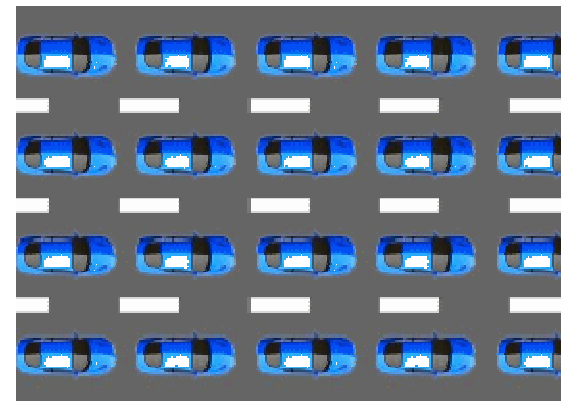


X. Chen, et al, [arXiv:1012.2783](https://arxiv.org/abs/1012.2783) (Birmingham, DTU, Imperial)

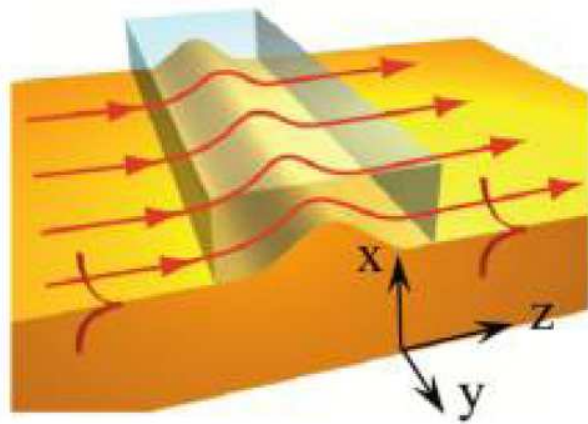
# Space-time Cloak – History Editor



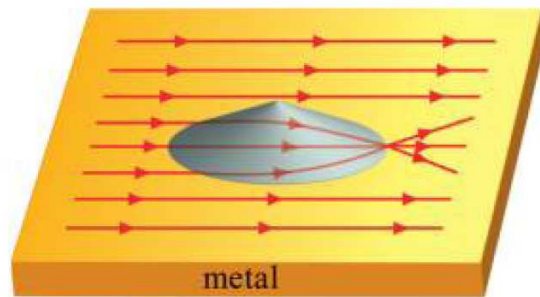
Star Trek transporter



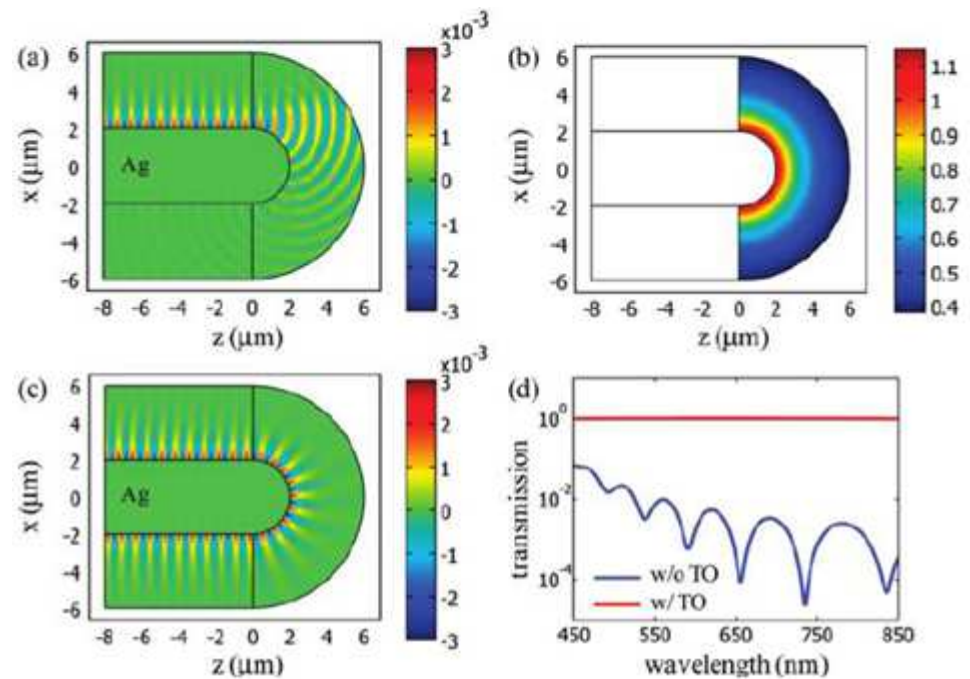
# Plasmonics Gets Transformed



SPP overcoming protrusion



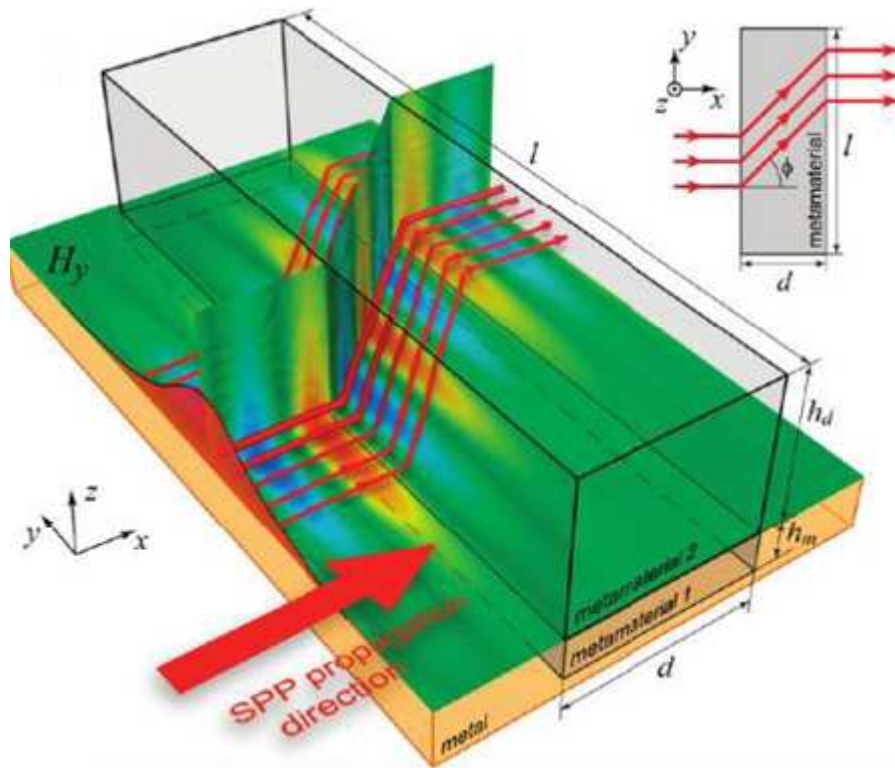
Plasmonic Luneburg lens



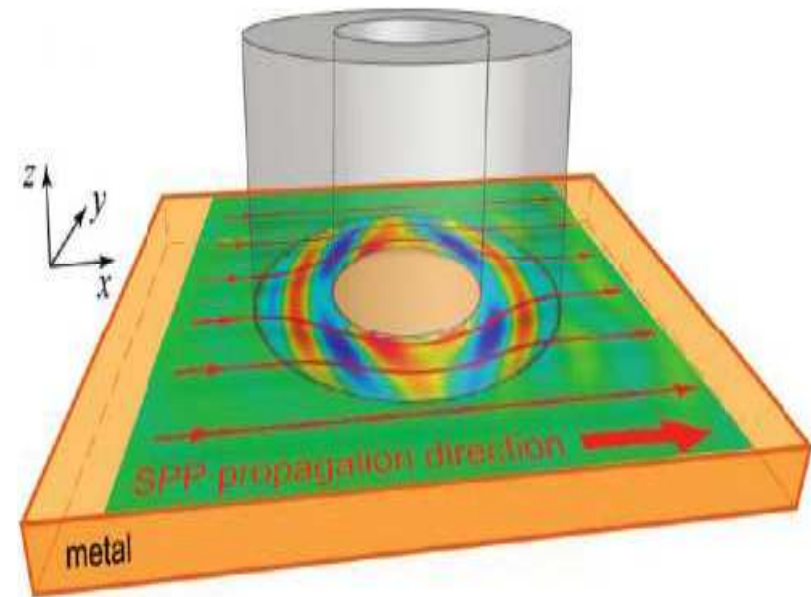
Plasmonic 180° waveguide bend



# Plasmonics Gets Transformed



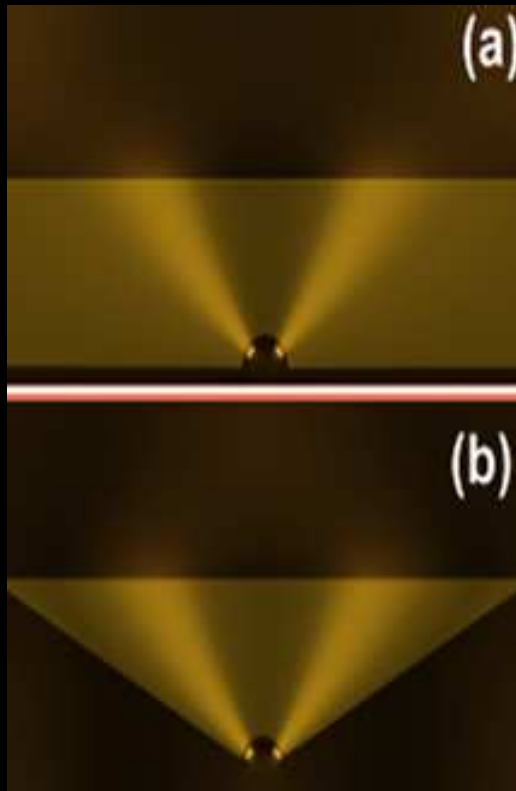
SPP beam shifter



Cylindrical cloak for SPPs

# Engineering Meta-Space for Light

Kildishev, VMS (*OL*, 2008); Shalaev, *Science* 322, 384 (2008)

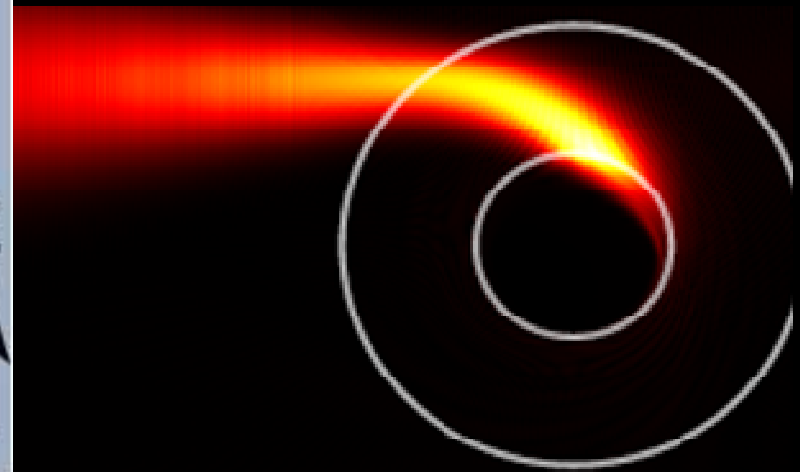


Planar hyperlens  
(Kildishev and VMS)  
(Schurig et al; Zhang group)



Light concentrator  
(also, Schurig et al)

*Fermat:*  $\delta \int n dl = 0$   
 $n = \sqrt{\epsilon(r)\mu(r)}$   
*curving optical space*



Optical Black Hole  
(Zhang group;  
Narimanov, Kildishev)

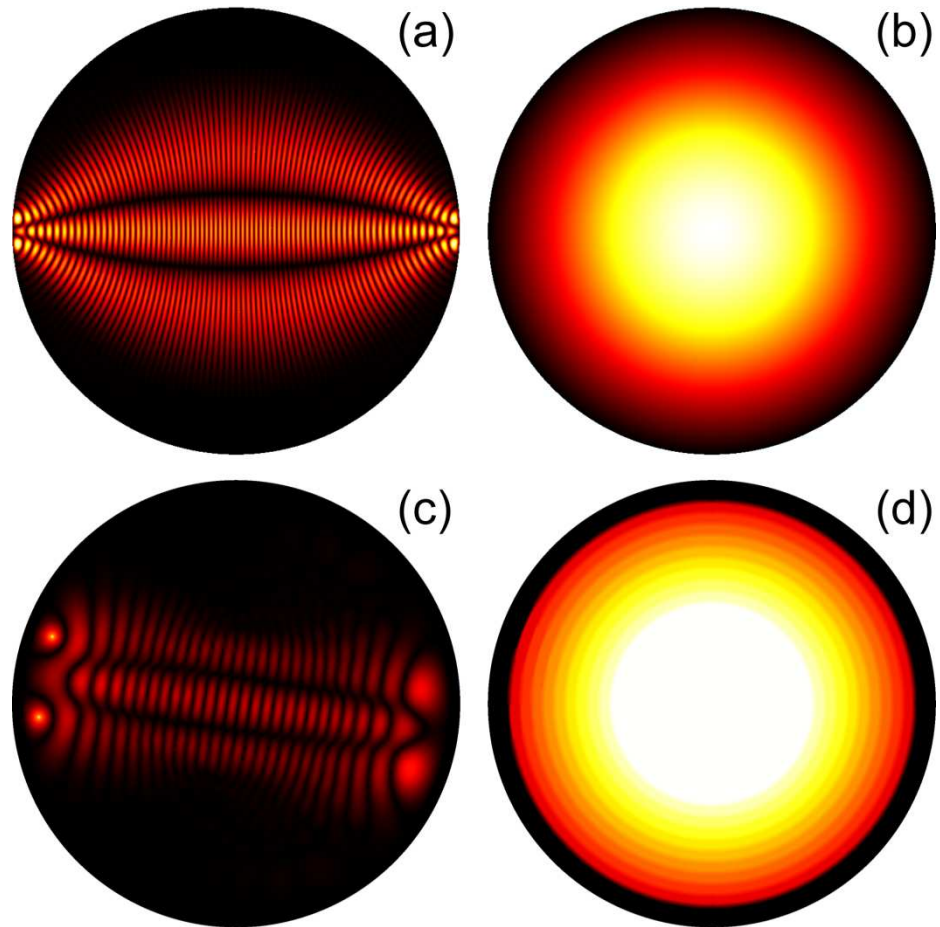
# **Maxwell Fisheye and Eaton Lenses Emulated by Microdroplets**

V.N. Smolyaninova, I.I. Smolayninov, A.V. Kildishev  
and V.M. Shalaev  
(Optics Letters 2010)

Other relevant work by Leonhard , et al.

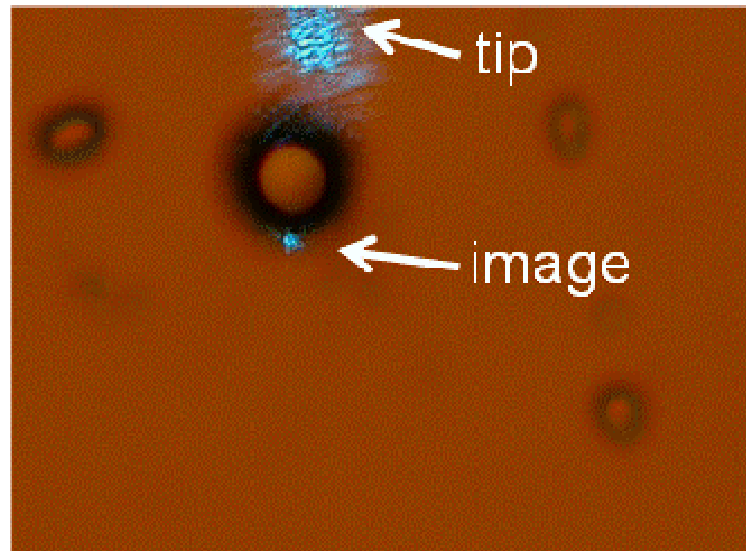
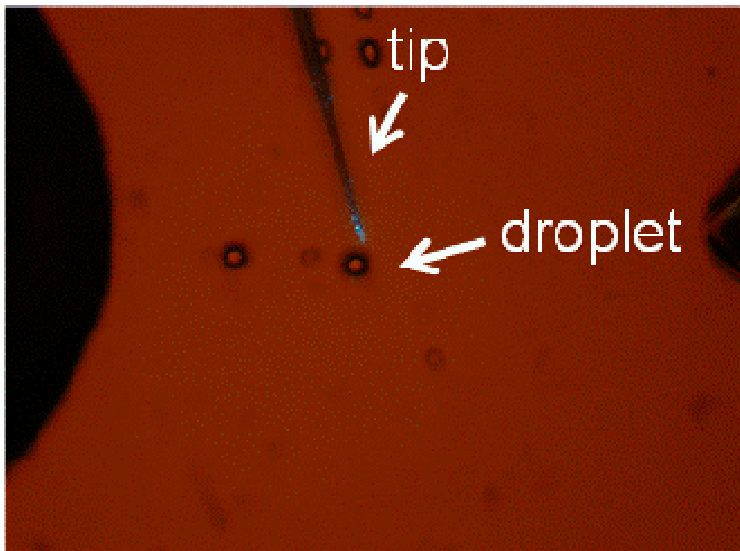
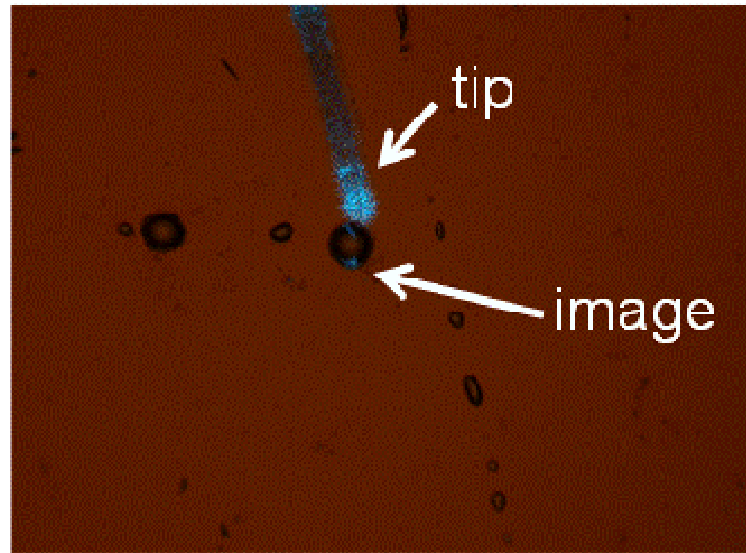
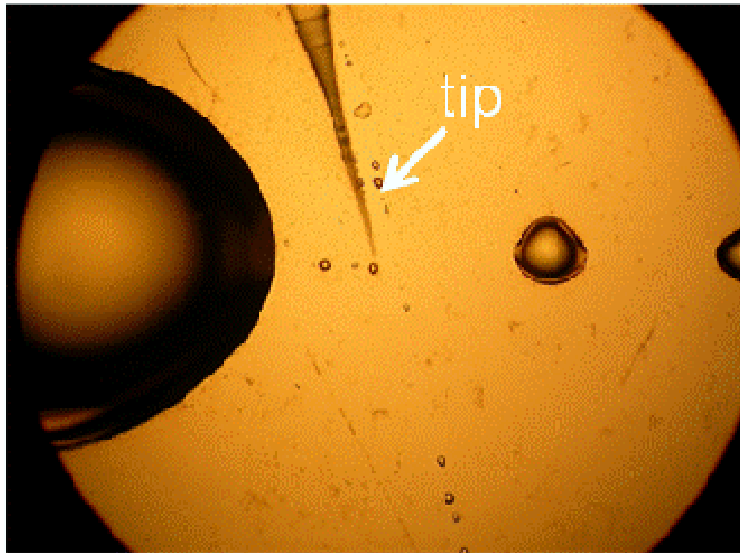
# Simulations of Fish Eye and Eaton Lenses

## Fish eye and Eaton lenses



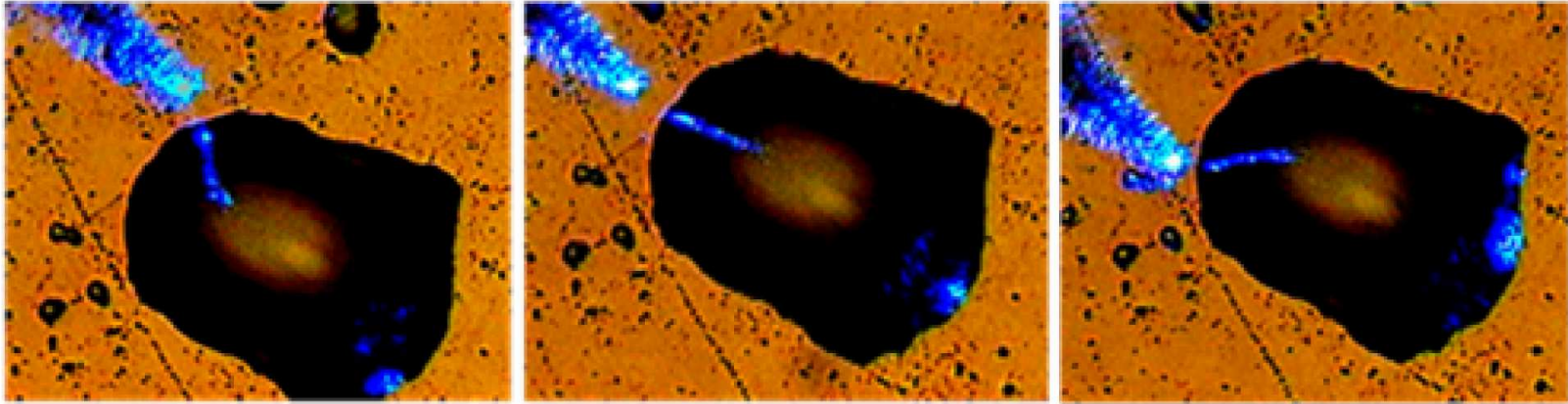
refractive index

# Fish Eye / Eaton Lens Based on a Droplet

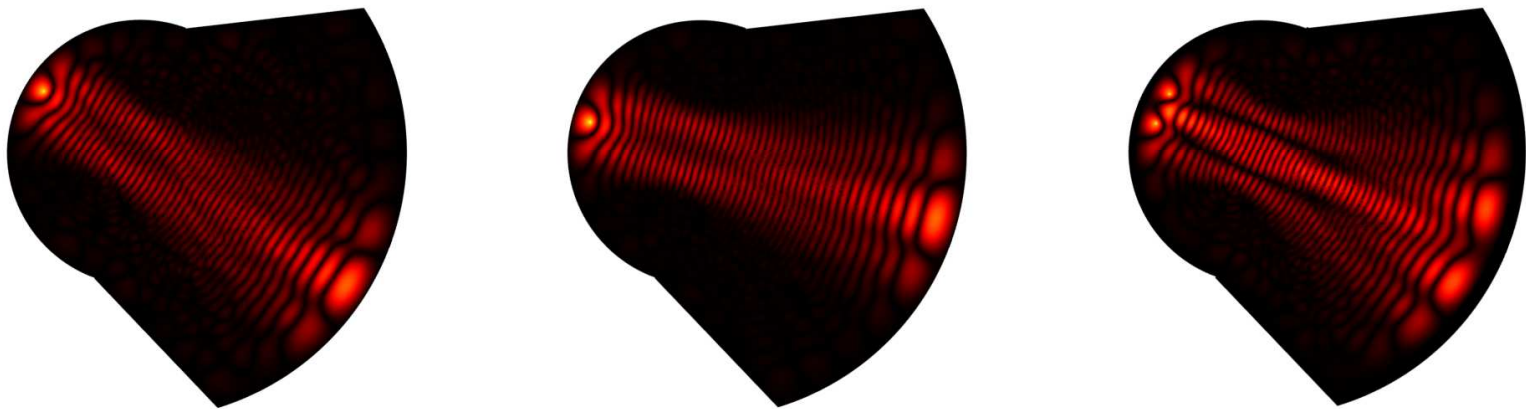


# Magnification with an Eaton Lens

Moving source close to the 'equator' as a proof of magnification



Magnification with Eaton lens





## Slide 57

---

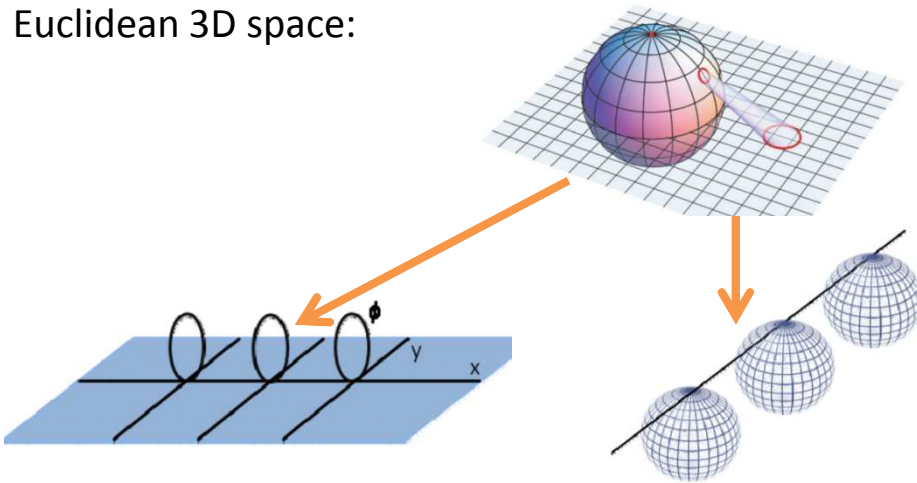
i22

We have created glycerin droplets with shapes, which are very close to the shape of the “deformed droplet” used in the numerical simulations. Image magnification of the “deformed droplet” has been tested by moving the near field microscope tip along the droplet edge, as shown in the top row. Image magnification appears to be close to the  $M=2$  value predicted by our simulations

igor.smolyaninov, 06/02/2010

# Metamaterial “Multiverse” (Smolyaninov)

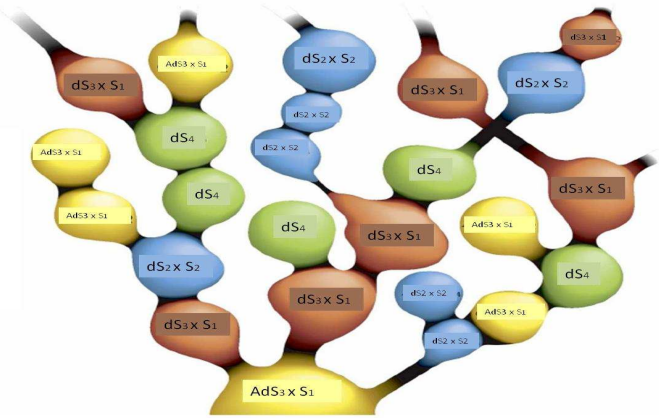
Using transformation optics we can create “optical spaces” having non-trivial topology, which cannot normally fit into Euclidean 3D space:



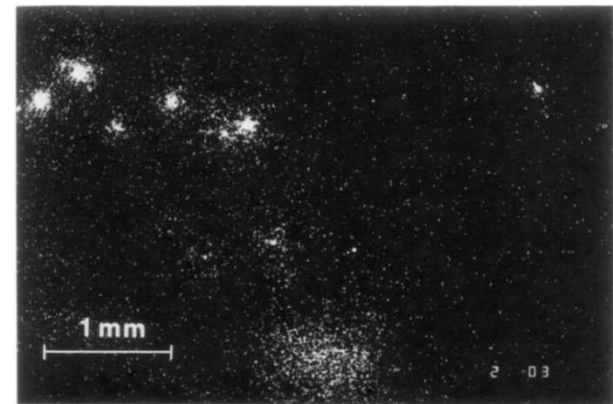
Even metric signature of the “optical space” may differ from the (+ - - -) signature of the Minkowski space. In hyperbolic materials (Smolyaninov, Narimanov – PRL, 2010):

$$\frac{\partial^2 \varphi}{c^2 \partial t^2} = \frac{\partial^2 \varphi}{\epsilon_1 \partial z^2} + \frac{1}{\epsilon_2} \left( \frac{\partial^2 \varphi}{\partial x^2} + \frac{\partial^2 \varphi}{\partial y^2} \right) \quad \begin{matrix} \epsilon_1 < 0 \\ \epsilon_2 > 0 \end{matrix}$$

$$\left( \frac{\partial^2}{\partial x_1^2} + \frac{\partial^2}{\partial x_2^2} - \frac{\partial^2}{\partial x_3^2} - \frac{\partial^2}{\partial x_4^2} \right) \varphi = 0 \quad \text{2T K-G}$$



Modern cosmology describes Universe as collection of spaces connected by black holes and wormholes. These spaces may have different topology and different number of dimensions.



Flashes of light are observed during metric signature transitions : toy Big Bang physics

Smolyaninov, J. of Optics (2011)

## Purdue “meta-strike force”



Published 2009

